

# Adsorption and Diffusion of Lithium and Sodium on Defective Rhenium Disulfide: A First Principles Study

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## S Supporting Information

**ABSTRACT:** Single-layer rhenium disulfide (ReS<sub>2</sub>) is a unique material with distinctive, anisotropic electronic, mechanical, and optical properties and has the potential to be used as an anode in alkali-metal-ion batteries. In this work, first principles calculations were performed to systematically evaluate the potential of monolayer pristine and defective ReS<sub>2</sub> as anodes in lithium (Li)- and sodium (Na)-ion batteries. Our calculations suggest that there are several potential adsorption sites for Li and Na on pristine ReS<sub>2</sub>, owing to its low-symmetry structure. Additionally, the adsorption of Li and Na over pristine ReS<sub>2</sub> is very strong with adsorption energies of −2.28 and −1.71 eV, respectively. Interestingly, the presence of point defects causes significantly stronger binding of the alkali-metal atoms with adsorption energies in the range −2.98 to −3.17 eV for Li and −2.66 to −2.92 eV for Na. Re single vacancy was found to be the strongest binding defect for Li adsorption, whereas S single vacancy was found to be the strongest for Na. The diffusion of these two alkali atoms over pristine ReS<sub>2</sub> is anisotropic, with an energy barrier of 0.33 eV for Li and 0.16 eV for Na. The energy barriers associated with escaping a double vacancy and single vacancy for Li atoms are significantly large at 0.60 eV for the double-vacancy case and 0.51 eV for the single-vacancy case. Similarly, for Na, they are 0.59 and 0.47 eV, respectively, which indicates slower migration and sluggish charging/discharging. However, the diffusion energy barrier over a Re single vacancy is found to be merely 0.42 eV for a Li atom and 0.28 eV for Na. Overall, S single and double vacancies can reduce the diffusion rate by 10<sup>3</sup>–10<sup>5</sup> times for Li and Na ions, respectively. These results suggest that monolayer ReS<sub>2</sub> with a Re single vacancy adsorbs Li and Na stronger than pristine ReS<sub>2</sub>, with negligible negotiation with the charging/discharging rate of the battery, and therefore they can be used as an anode in Li- and Na-ion batteries.

**KEYWORDS:** Li/Na-ion battery, density functional theory, ReS<sub>2</sub>, specific capacity, adsorption and diffusion

## 1. INTRODUCTION

With the ever-increasing demand for light, and eco-friendly batteries with high power and energy densities,<sup>1,2</sup> low self-discharge rate, and comparatively long-term cycling stability<sup>3</sup> for running mobile devices and electrical vehicles (EVs), scientists are in constant search of suitable electrode materials. Alkali-metal (Li, Na)-ion batteries (AIBs) are potential candidates for the next-generation energy technology as they are portable, energy-efficient, and environmentally friendly.<sup>4,5</sup> The challenge associated with applying alkali-metal-ion batteries to EVs and portable appliances is obtaining a large storage capacity without compromising their long cycle lives and high charging/discharging rates.<sup>6</sup> The latter is determined by the ionic mobilities of alkali-metal ions in the electrode materials of the battery, which depend on the electronic interactions between the electrode and the alkali-metal ion.

Thus, performance of these batteries is primarily dependent on the quality of the electrodes used. The performance of commercial lithium-ion batteries (LIBs), which use graphitic materials, oxides, and oxysalts as anode materials, is limited due to their poor power density arising from the low diffusivity of Li atoms within them. Practical solutions to some of these problems is to use anode materials with large surface areas and high Li atom diffusivities. In this regard, theoretical and experimental studies have reported that two-dimensional (2D) materials can be effectively used as anode materials in AIBs due to their large surface-to-volume ratios and exceptional electronic and mechanical properties. For example, alkali-

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metal-ion batteries with anodes based of 2D materials, such as graphene,<sup>7,8</sup> phosphorene,<sup>9–11</sup> and borophene,<sup>12,13</sup> have been investigated because of their excellent electrochemical performance as battery electrodes. In particular, graphene anodes have been demonstrated to possess capacities in the range of 600 mAh/g compared to a theoretical capacity of 372 mAh/g for graphite-based LIBs.<sup>7</sup>

In the recent past, 2D transition-metal dichalcogenides (TMDs), which combine transition metals and chalcogenides, have attained increased attention from the electrode development community.<sup>14–17</sup> TMDs are layered structures, wherein different layers are held together by weak van der Waals forces. Unlike other 2D TMDs, ReS<sub>2</sub> has a direct band gap (1.47–1.61 eV)<sup>18</sup> and demonstrates a naturally distorted octahedral (1T) structure with a triclinic lattice, which provides unique chemical and electronic properties due to the lowered structural symmetry.<sup>19</sup> In bulk ReS<sub>2</sub>, different atomic layers act electronically and vibrationally dissociated. As a result, the interlayer spacing in 2D ReS<sub>2</sub> is about 0.65–0.7 nm, compared to 0.33 nm for graphite, whereas the interlayer coupling energy is 18 meV compared to 460 meV in MoS<sub>2</sub>.<sup>20</sup> Consequently, relatively large Li ions can migrate rapidly through ReS<sub>2</sub> without significant volumetric expansion, a problem critical to Si-based LIB anodes.<sup>21</sup> Recent experiments have demonstrated that LIBs made of ReS<sub>2</sub>/graphene composites and few layers of ReS<sub>2</sub>/carbon nanotube-based nanosheets possess capacities in the range of 300–900 mAh/g.<sup>22,23</sup> Additionally, we have recently demonstrated that vertically oriented arrays of ReS<sub>2</sub> nanosheets hold exceptional potential for use in Li–S batteries for energy storage.<sup>24</sup>

Ever since the discovery of monolayer ReS<sub>2</sub>,<sup>20</sup> several top-down exfoliation-based techniques have been utilized for its synthesis, such as top-down mechanical exfoliation<sup>25,26</sup> and intercalation exfoliation<sup>27</sup> from its bulk counterparts. Additionally, chemical vapor deposition (CVD),<sup>28,29</sup> chemical vapor transport,<sup>20,29</sup> metal sulfurization,<sup>30</sup> and plasma-assisted method<sup>31</sup> have all been successfully utilized to fabricate 2D ReS<sub>2</sub>. Generally, synthesis of 2D materials from bulk structures using deposition techniques or exfoliation comes at the cost of creating lattice defects in the final structure, such as point defects, and grain boundaries.<sup>29</sup> Thus, these structural defects alter the mechanical and electronic properties of the 2D structure significantly. For example, CVD-grown MoS<sub>2</sub> possesses inferior carrier mobility compared to their exfoliated counterparts. Also, point defects have been demonstrated to alter the magnetic properties of ReS<sub>2</sub><sup>32</sup> and NbSe<sub>2</sub>.<sup>33</sup> significantly. It has been reported that point defects in graphene<sup>34</sup> and MoS<sub>2</sub><sup>35</sup> increase the adsorption capability of Li ions and therefore increase the storage capacity of the battery. However, this increased adsorption strength can affect the diffusivity of the Li ions in the electrode due to increased chemical interaction between the substrate and the Li ions. For example, Sun et al.<sup>35</sup> reported that Li ions diffusion rates remain almost unaffected in MoS<sub>2</sub> with point defects and grain boundaries. In graphene, on the other hand, the rate of diffusion of Li atoms is more pronounced along a grain boundary compared to a direction perpendicular to the boundary.<sup>36</sup> Additionally, the rate of diffusion of Na over grain boundaries in graphene is more preferable over pristine graphene.<sup>37</sup> On the contrary, Zhang et al.<sup>38</sup> reported that single vacancies and double vacancies block the migration of Li ions over black phosphorous. These contradictions with different materials have lead us to raise the question of how lattice

defects influence the adsorption and charging/discharging rates of Li and Na atoms in ReS<sub>2</sub>-based batteries.

In this paper, the adsorption and diffusion of Li and Na atoms over ReS<sub>2</sub> via first principles density function theory (DFT) calculations have been reported. To the best of our knowledge, the adsorption and diffusion of Li and Na over defective ReS<sub>2</sub> have not been studied before. First, the favorable adsorption sites for the metal ions over pristine ReS<sub>2</sub> were identified, followed by the favorable adsorption sites for defective ReS<sub>2</sub> surfaces. Three distinct point defects, namely, sulfur single vacancy (SV), rhenium single vacancy, and sulfur double vacancy (DV), were created in the ReS<sub>2</sub> monolayers. These vacancies have been created in accordance with a previous DFT study on the stability and formation of point defects in ReS<sub>2</sub>.<sup>39,39</sup> Our calculations showed that binding energies for Li and Na atoms increase over defective ReS<sub>2</sub> compared to pristine monolayers. Additionally, charge density difference analysis and partial density of states calculations were performed to gain further insights into the adsorption process and characterize the electronic properties of Li- and Na-stuffed ReS<sub>2</sub> monolayers. Finally, climbing image nudged elastic band (CI-NEB) simulations were performed to determine the minimum-energy pathways (MEPs) and associated energy barriers for the Li and Na atoms adsorbed onto the surface of ReS<sub>2</sub>.

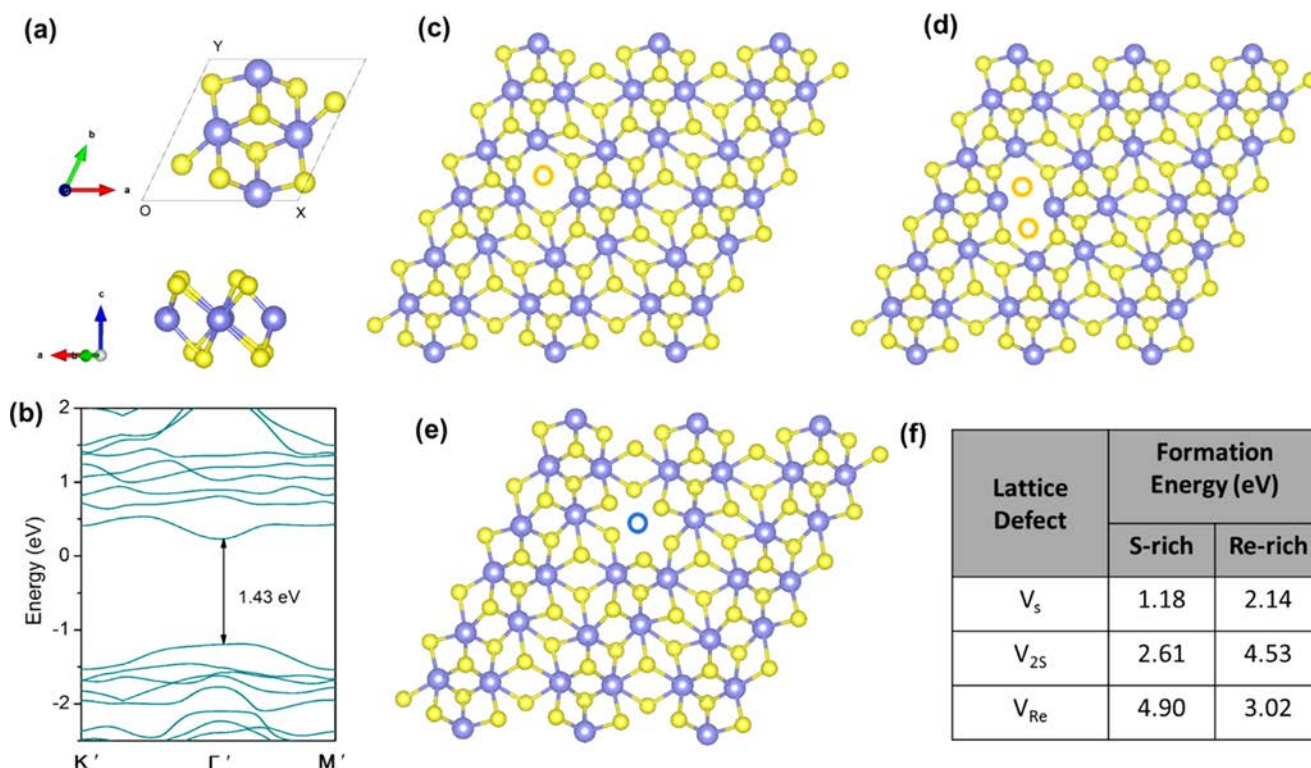
## 2. COMPUTATIONAL METHODS

Plane-wave-based DFT simulations were conducted using the Perdew–Burke–Ernzerhof (PBE)<sup>40</sup> exchange–correlation functional within the generalized gradient approximation using the Quantum ESPRESSO package.<sup>41</sup> In addition, the Heyd–Scuseria–Ernzerhof (HSE06) functional was used to compute the band gap of pristine ReS<sub>2</sub>. The atomic positions and lattice constants were optimized using the kinetic energy cutoff of 60 Ry for the wave functions and 480 Ry for the charge density, respectively. The convergence criterion of the self-consistent field procedure was set to  $1 \times 10^{-6}$  Ry. To avoid any interlayer interactions between ReS<sub>2</sub> surfaces from long-range van der Waals forces due to periodicity, a convergence test with respect to the box dimension in the *z* direction was performed (see Table S1), and a vacuum spacing of 15 Å was deemed sufficient. For binding energy computations, the position of every atom was relaxed using a conjugate gradient minimization over a  $4 \times 4 \times 1$  Monkhorst–Pack<sup>42</sup> grid of *k*-points with the residual Hellmann–Feynman force on each atom less than 0.001 Ry/b. For structural analysis, all of the structures were visualized with XCrySDen<sup>43</sup> and VESTA.<sup>44</sup> The pristine ReS<sub>2</sub> supercell consisted of  $2 \times 2$  unit cells (with 48 atoms), whereas the single-vacancy (SV) and double-vacancy (DV) supercells consisted of  $3 \times 3$  unit cells (107 and 106 atoms, respectively). When calculating the adsorption energies of adsorbents over pristine and defective ReS<sub>2</sub>, the dispersion corrections due to van der Waals forces were accounted by adopting the DFT + D approach.<sup>45</sup> To find the most stable adsorption positions, the alkali-metal atoms were placed above the sulfur atoms at different sites, followed by relaxation. The most stable adsorption site was determined by a comparison of the adsorption energies. The adsorption energy ( $E_{ad}$ ) and charge density difference ( $\rho_{ad}$ ) are determined by

$$E_{ad} = E_{\text{adsorbed state}} - (E_{\text{adsorbent}} + E_{\text{substrate}}) \quad (1)$$

$$\rho_{ad} = \rho_{\text{adsorbed state}} - (\rho_{\text{adsorbent}} - \rho_{\text{substrate}}) \quad (2)$$

where  $E_{\text{adsorbed state}}$  represents the energy of monolayer ReS<sub>2</sub> after the adsorption of an alkali-metal atom,  $E_{\text{adsorbent}}$  represents the energy of a single alkali-metal atom, and  $E_{\text{substrate}}$  represents the energy of the monolayer ReS<sub>2</sub>. A negative adsorption energy indicates that the adsorption is spontaneous and energetically favorable, with smaller values suggesting a stronger binding. Similarly,  $E_{\text{adsorbed state}}$  is the



**Figure 1.** (a) Top view and side view of the unit cell of  $\text{ReS}_2$ . (b) Band structure of pristine  $\text{ReS}_2$ , with a band gap of 1.43 eV. Configurations of point defects in monolayer  $\text{ReS}_2$ . Top view of optimized structures of (c)  $V_S$ , (d)  $V_{2S}$ , and (e)  $V_{Re}$ . Hollow circles represent S (yellow) and Re (blue) atoms removed from the monolayer  $\text{ReS}_2$ . (f) Formation energies associated with the lattice defects under both S-rich and Re-rich conditions.

charge density of  $\text{ReS}_2$  monolayer after alkali-metal adsorption,  $\rho_{\text{adsorbent}}$  is the charge density of an alkali-metal atom, and  $\rho_{\text{substrate}}$  represents the charge density of monolayer  $\text{ReS}_2$ . The average adsorption energy ( $E_{\text{avg}}$ ) is calculated using the following equation

$$E_{\text{avg}} = \frac{E_{\text{adsorbed state}} - n \times E_{\text{adsorbent}} - E_{\text{substrate}}}{n} \quad (3)$$

where  $n$  represents the number of Li and Na atoms adsorbed,  $E_{\text{adsorbed state}}$  represents the energy of the system after adsorption of all of the Li/Na atoms,  $n \times E_{\text{adsorbent}}$  represents the total energy of the Li or Na atoms, and  $E_{\text{substrate}}$  represents the energy of pristine  $\text{ReS}_2$ . The open-circuit voltage (OCV) of the secondary battery is related to the total energy storage of the battery. As shown in previous works, this parameter may be estimated using the following relation under the assumption that volume and entropic terms are negligible<sup>46–48</sup>

$$\text{OCV} \approx \frac{-E_{\text{avg}}}{e} \quad (4)$$

where  $e$  is the elementary charge. The storage capacity of  $\text{ReS}_2$  can be calculated using Faraday's equation, given by

$$q = 1000 \times F \times z \frac{n}{M_{\text{ReS}_2}} \quad (5)$$

where  $F$ ,  $n$ ,  $M_{\text{ReS}_2}$ , and  $z$  are Faraday's constant, the number of electrons involved in the electrochemical reaction, the mass of  $\text{ReS}_2$ , and the number of valence electrons involved in the electrochemical process, respectively. For studying the kinetics of diffusion of the adsorbent atoms over pristine and defective  $\text{ReS}_2$  monolayers and calculating the associated energy barriers of diffusion, the climbing image nudged elastic band (CI-NEB) method<sup>49</sup> was utilized.

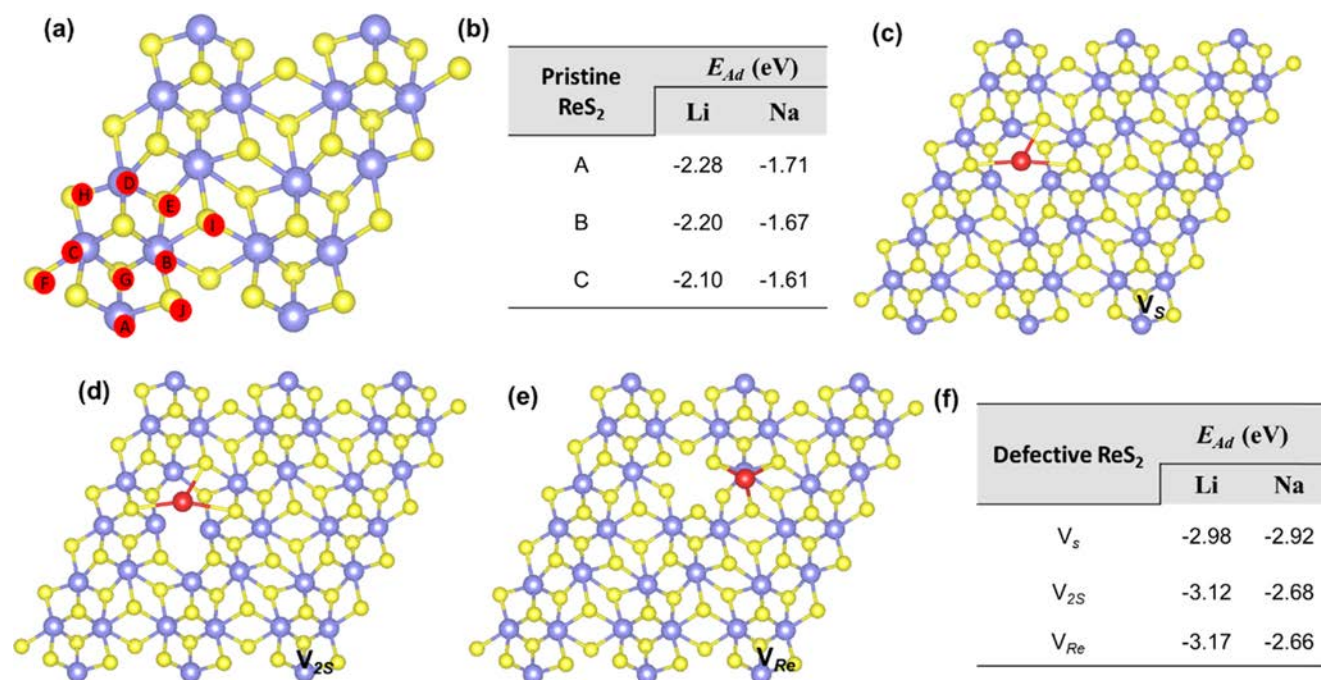
### 3. RESULTS AND DISCUSSION

**3.1. Structure of Pristine and Defective  $\text{ReS}_2$ .** Before discussing distinctive characteristics of alkali-metal adsorption

over pristine and defective  $\text{ReS}_2$ , their relative stabilities and structural aspects are presented here. Unlike other TMDs, which have stable 1 hexagonal (H) (dichalcogens of Mo and W) and 1T (dichalcogens of Ti, V, and Ta) phases,  $\text{ReS}_2$  has a distorted (1Td) phase, wherein four Re atoms group into  $\text{Re}_4$  units to form  $\text{ReS}_2$ .<sup>39</sup> Tongay et al. calculated the phonon dispersion using the PBE functional and compared the results with experimental measurements of Raman spectra in  $\text{ReS}_2$ .<sup>40</sup> They showed that weaker interlayer interaction leads to decoupling of lattice vibrations between subsequent layers of  $\text{ReS}_2$ . Additionally, unlike other transition-metal dichalcogenides (TMDs), the LA and ZA phonon modes of periodic 1H and 1T structures of  $\text{ReS}_2$  have imaginary frequencies and therefore are dynamically unstable. The distorted structure of 2D  $\text{ReS}_2$  provides unique chemical and electronic properties. The distortion creates rhenium–sulfide bonds of varying lengths, with no single sulfur atom being in direct alignment with the ones surrounding it. In this study, the optimized parameters of the  $\text{ReS}_2$  unit cell (Figure 1a) were found to be:  $OX = 6.54 \text{ \AA}$ ,  $OY = 6.44 \text{ \AA}$ , and  $\angle XOY = 61.15^\circ$ .<sup>9</sup> The band diagram for pristine  $\text{ReS}_2$  is shown in Figure 1b, which suggests a band gap of 1.43 eV. This band gap of  $\text{ReS}_2$  is in excellent agreement with previous reports.<sup>20</sup> Because the PBE functional is known to underestimate band gap, HSE06 hybrid functional was used to obtain a more accurate electronic structure, which yielded a band gap of 2.41 eV for pristine  $\text{ReS}_2$ .

Due to its distorted structure, creating a defect at one site on the  $\text{ReS}_2$  surface is not the same as creating a defect at another site. Thus,  $\text{ReS}_2$  can have a vast variety of single and double vacancies of S and Re. Notably, whenever a vacancy defect is introduced on the  $\text{ReS}_2$  surface, a substantial change in the overall structure occurs. The energetics and lattice structures of





**Figure 2.** (a) Top view of the most stable sites for the adsorption of Li and Na over monolayer pristine ReS<sub>2</sub>. (b) Comparison of adsorption energies of Li and Na over pristine ReS<sub>2</sub> for three most favorable active sites. Most stable sites for Li and Na adsorption over (c)  $V_S$ , (d)  $V_{2S}$ , and (e)  $V_{Re}$ . Color code for atoms: yellow, S; violet, Re; red, Li and Na. (f) Adsorption energies of Li and Na over  $V_S$ ,  $V_{2S}$ , and  $V_{Re}$ .

point defects in anisotropic ReS<sub>2</sub> are distinct from those in isotropic binary honeycomb-like TMDs, such as MoS<sub>2</sub> and VS<sub>2</sub>.<sup>39</sup> For example, using high-resolution transmission electron microscopy and Raman spectroscopy, Wu et al.<sup>29</sup> identified and characterized the grain boundary structure in ReS<sub>2</sub> nanofilms and demonstrated that a variety of clusters and single, double, and triple vacancies are formed, which are complex in comparison to defect structures reported for other 2D systems.

Commonly observed point defects in ReS<sub>2</sub> are monosulfur vacancy ( $V_S$ ), disulfur vacancy ( $V_{2S}$ ), and single-metal vacancy ( $V_{Re}$ ). Horzum et al.<sup>39</sup> systematically studied the energetics of different point defects in ReS<sub>2</sub> and found that the stability of the defects are site-dependent. They reported that the most stable single S vacancy in ReS<sub>2</sub> is obtained by removing a S atom from ReS chains (Figure 1c). The most stable  $V_{2S}$  is created by removing two S atoms from the same sublattice, i.e., by removing another S atom neighboring the  $V_S$  (Figure 1d). Although two possible sites exist for creating  $V_{Re}$ , the one with the lowest formation energy is shown in Figure 1e. The relative stability of different point defects in a system is determined in terms of the formation energy of the defect, which is given by

$$E_f = E_{def} - E_{pristine} + \sum_i N\mu_i \quad (6)$$

where  $E_{def}$  and  $E_{pristine}$  are the total energies of the defective and pristine supercells,  $N$  is the number of  $i$ th atoms removed from the pristine surfaces to create defects, and  $\mu_i$  is the chemical potential of the  $i$ th species in its stable bulk form. Under thermal equilibrium, the chemical potential of ReS<sub>2</sub> monolayer satisfies  $\mu_{ReS_2} = \mu_{Re} + 2\mu_S$ , where  $\mu_{Re}$  and  $\mu_S$  are the chemical potentials for Re and S, respectively. For a Re-rich environment,  $\mu_{Re} = E_{tot}(Re)$ , where  $E_{tot}(Re)$  is the total energy of a Re atom in the bulk form. Thus,  $\mu_S = (\mu_{ReS_2} - \mu_{Re})/2$ . Under S-rich condition,  $\mu_S = E_{tot}(S)$ , where  $E_{tot}(S)$  is the energy of a S atom in the bulk form. Therefore,  $\mu_{Re}$  can be calculated as  $\mu_{Re} = \mu_{ReS_2}$

–  $2\mu_S$ . The formation energies for  $V_S$ ,  $V_{2S}$ , and  $V_{Re}$  are 1.18, 2.61, and 4.9 eV under S-rich conditions and 2.14, 4.53, and 3.02 eV under Re-rich condition, respectively (Figure 1f). These magnitudes of formation energies agree with those reported in ref 39. The formation energy of  $V_S$  is the lowest under both Re-rich and S-rich conditions, which suggests that sulfur single vacancies are most likely to form during mechanical exfoliation. This behavior is similar to MoS<sub>2</sub>, in which  $V_S$  is the most energetically favored point defect but is unlike graphene, wherein carbon double vacancy is the most favored point defect. Also, since the formation energy of  $V_{2S}$  is larger than twice that of  $V_S$ , two separate  $V_S$  would not combine to create a disulfur  $V_{2S}$  vacancy. Additionally, the Re single vacancy has the largest formation energy compared to  $V_S$  even under a S-rich condition. At a finite temperature,  $T$ , the areal density of defects is related to the formation energy of the defect and can be calculated using an Arrhenius-type equation given by

$$N_{defect} = N_{pristine} \exp\left(-\frac{E_f^T}{k_B T}\right) \quad (7)$$

where  $N_{pristine}$  is the areal density of atoms in the pristine material,  $E_f^T$  is the formation energy of the defect at  $T$ ,  $k_B$  is the Boltzmann constant. Temperature-dependent magnitudes of  $E_f^T$  can be calculated by performing ab initio molecular dynamics simulations.

**3.2. Adsorption of Li and Na on Pristine and Defective ReS<sub>2</sub>.** Pristine ReS<sub>2</sub> is anisotropic, which gives rise to several asymmetric adsorption sites favorable for lithiation and sodiation. The binding energies for the adsorption of Li and Na atoms for a set of 10 active sites over monolayer pristine ReS<sub>2</sub> surface have been evaluated. The equilibrium positions for Li and Na atoms were determined by first placing the adatoms 3.5 Å away from the ReS<sub>2</sub> surface and subsequently optimizing

the structure by minimizing the overall energy. DFT calculations show that site-A with  $E_{\text{ad}} = -2.28$  eV for Li and  $-1.71$  eV for Na is the most favorable location for both lithiation and sodiation over pristine  $\text{ReS}_2$ . The metal atoms prefer to reside near the area in between three sulfur atoms. For the adsorption of Li over site-B and site-C, the magnitudes of  $E_{\text{ad}}$  are  $-2.2$  and  $-2.1$  eV, respectively. The adsorption energy of Li over site-A is  $0.89$  eV higher than that of  $\text{SnS}_2$ ,<sup>14</sup>  $0.26$  eV higher than that of  $\text{GeS}$ ,<sup>50</sup>  $0.1$  eV higher than that of  $\text{MoS}_2$ .<sup>35</sup> Similarly, the adsorption energy of Na over site-A is  $1.3$  eV higher than that of pentagraphene,<sup>51</sup>  $0.35$  eV higher than that of  $\text{GeS}$ ,<sup>50</sup> and  $0.2$  eV higher than that of  $\text{Ti}_3\text{C}_4$ .<sup>52</sup> The adsorption energies for Na over site-B and site-C are  $-1.67$  and  $-1.61$  eV, respectively. Equilibrium configurations and binding energies of Li and Na adsorption over site-A, site-B, and site-C are also presented in Figure 2a,b, with the corresponding charge density difference contours presented in Figures S1 and S2. The binding energies of Li and Na over all of the 10 sites are presented in Table S2. Negative adsorption energies for a range of adsorption sites indicate that Li and Na storage over pristine  $\text{ReS}_2$  is a spontaneous process, which is an essential requirement for alkali-metal-ion batteries. Also, the binding energy associated with the adsorption of Li and Na is the largest near the Re chains. Thus, the adatoms atoms tend to accumulate near these Re chains.

Previous studies of Li adsorption on 2D materials suggest that metal adatoms tend to get adsorbed adjacent to the defective zone because of the unused electrons from the dangling bonds.<sup>37,38</sup> To find the best adsorption sites for Li and Na onto defective  $\text{ReS}_2$ , a host of initial positions for the adatoms were considered around the defective sites, the strongest adsorption sites, and the corresponding adsorption energies are shown in Figure 2c–f. On defective  $\text{ReS}_2$ , Li and Na atoms prefer to get adsorbed in the hollow site between two S atoms. For example, in the case of  $V_{\text{S}}$  (Figure 2c), both Li and Na prefer to bind directly over the vacancy, suggesting it has taken the place of the sulfur atom. The binding energies for Li and Na over  $V_{\text{S}}$  are  $2.98$  and  $2.92$  eV, respectively. In the case of  $V_{2\text{S}}$  (Figure 2d), the metal atoms prefer to adsorb onto a similar position, with binding energies of  $-3.12$  and  $2.68$  eV for Li and Na, respectively. The adsorption of a Li atom over monolayer  $\text{ReS}_2$  with a  $V_{\text{Re}}$  (Figure 2e) is the strongest with a binding energy of  $-3.17$  eV, compared to a binding energy of  $-2.28$  eV for pristine  $\text{ReS}_2$ . However, in the case of  $V_{\text{Re}}$ , the metal atoms tend to get adsorbed over site-A close to  $V_{\text{Re}}$  rather than the hollow site created by the vacancy. Binding energies, the shortest distance between the adsorbent atoms and the Re and S atoms in pristine and defective  $\text{ReS}_2$  are presented in Table 1. Charge density difference contours for Li and Na adsorption over defective  $\text{ReS}_2$  are presented in Figures S3 and S4.

**Table 1. Adsorption Energies ( $E_{\text{ad}}$ ), the Shortest Distance between Li Atom at Neighboring Re Atom ( $d_{\text{Li-Re}}$ ) and S Atom ( $d_{\text{Li-S}}$ ) for Pristine,  $V_{\text{S}}$ ,  $V_{2\text{S}}$ , and  $V_{\text{Re}}$  Monolayer  $\text{ReS}_2$**

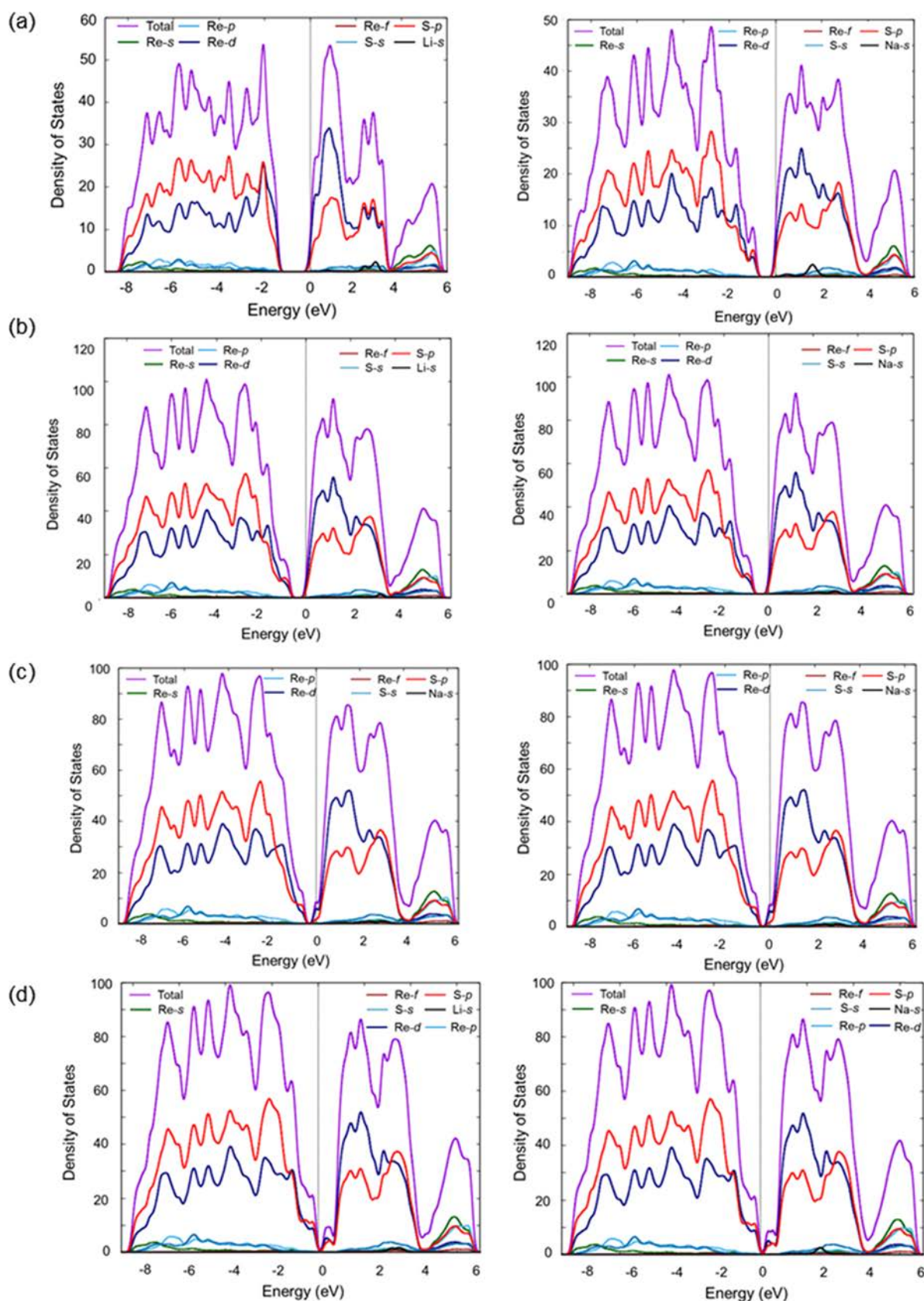
$E_{\text{ad}}$ (eV)	adsorbent	pristine	$V_{\text{S}}$	$V_{2\text{S}}$	$V_{\text{Re}}$
$d_{\text{Li-Re}}$ (Å)	Li	2.28	2.98	3.12	3.17
	Na	1.71	2.92	2.68	2.66
$d_{\text{Li-S}}$ (Å)	Li	2.95	2.78	2.73	2.89
	Na	2.93	3.14	3.07	3.46
$d_{\text{Li-S}}$ (Å)	Li	2.26	2.59	2.48	2.30
	Na	3.96	2.82	2.77	2.71

Additionally, Bader charge analysis<sup>53</sup> was conducted to quantify the charge-transfer process and understand the nature of interaction between the substrate (pristine and defective) and the adatoms, the details of which are presented in Figure S5.

To better understand the adsorption mechanism and ensure that the ideal electrode characteristics of  $\text{ReS}_2$  are retained, the projected density of states (PDOS) of all bound systems were calculated, as shown in Figure 3. As Li and Na atoms adsorb over pristine, and defective  $\text{ReS}_2$  monolayers, they provide some electronic states to each system and act as electron-donor species. The Li and Na 2s states are found deep in the conduction band, in all  $\text{ReS}_2$  systems, at energy levels corresponding to the magnitude of their respective binding energies. The adsorption of Li and Na in turn pushes the Fermi level to higher energies, n-doping all of the  $\text{ReS}_2$  systems. After the adsorption of Li and Na, the Fermi levels of pristine,  $V_{\text{S}}$ , and  $V_{2\text{S}}$   $\text{ReS}_2$  monolayers are found at the bottom of the conduction band, increasing the free-electron concentration, giving rise to n-type semiconducting monolayers. The adsorption of Na on the pristine  $\text{ReS}_2$  monolayer also closes the band gap between the valence and conduction bands, decreasing it to  $\sim 0.6$  eV. After the adsorption of Li and Na on the  $V_{\text{Re}}$   $\text{ReS}_2$  monolayer, the Fermi level is found at the top of valence band. The adsorption of Li and Na atoms decreases the conducting hole concentration, due to the n-doping, pushing the Fermi level to higher energies. However, at higher Li and Na concentrations, the Fermi level can be expected to increase to the bottom of the conduction band, creating an n-type semiconducting monolayer, increasing the free-electron concentration. The increase in free-electron concentration in all  $\text{ReS}_2$  monolayer systems may increase their electrical conductivity and potentially enhance their electrode performance.

Throughout the charging/discharging process, the concentration of the metallic ions in alkali-metal-ion batteries changes, resulting in compositional changes. Depending on the concentration of the alkali atoms, the adsorption sites vary, which is why it is important to study the effect of composition on the adsorption over pristine monolayer  $\text{ReS}_2$ . Additionally, for commercial purposes, the OCV is widely used for characterizing the performance of alkali-metal-ion batteries, such as the state of charge and health. OCV can be evaluated by estimating the voltage for a range of metal atoms stoichiometry. Here, to find  $E_{\text{avg}}$ , OCV, and specific capacity of pristine  $\text{ReS}_2$  as a function of Li and Na concentration, a  $2 \times 2$  supercell (16 Re atoms, 32 S atoms) is considered. Simulations were performed for a range of initial arrangements of Li and Na atoms. Initially, the adatoms were placed over site-A, site-B, or site-C, away from each other to avoid interactions of the adsorbent atoms. All of the structures are then fully optimized. The alkali atoms can be adsorbed until the average binding energy of each Li atom reaches 0 eV; however, for larger concentrations of the alkali atoms, the Re–S bonds may become weak or can fail, and they cannot rebuild and the charging/discharging process becomes irreversible. Therefore, low alkali atom concentrations have been considered here. Different compositions of  $\text{Li}_x\text{ReS}_2$  and  $\text{Na}_x\text{ReS}_2$  were studied with  $x$  taking on values of 0.125, 0.25, 0.375, 0.5, 1, 1.25, 1.5, 2, 2.5, and 4. Simulations show that the electrostatic repulsive force between the metal atoms increases progressively as the number of adatoms is increased. This leads to increasingly weaker adsorption. The highest Li/Na concentration is a 4:1 ratio between the adatoms and  $\text{ReS}_2$  (i.e.,  $\text{Li}_4\text{ReS}_2$  and  $\text{Na}_4\text{ReS}_2$ ), which leads to a specific capacity of

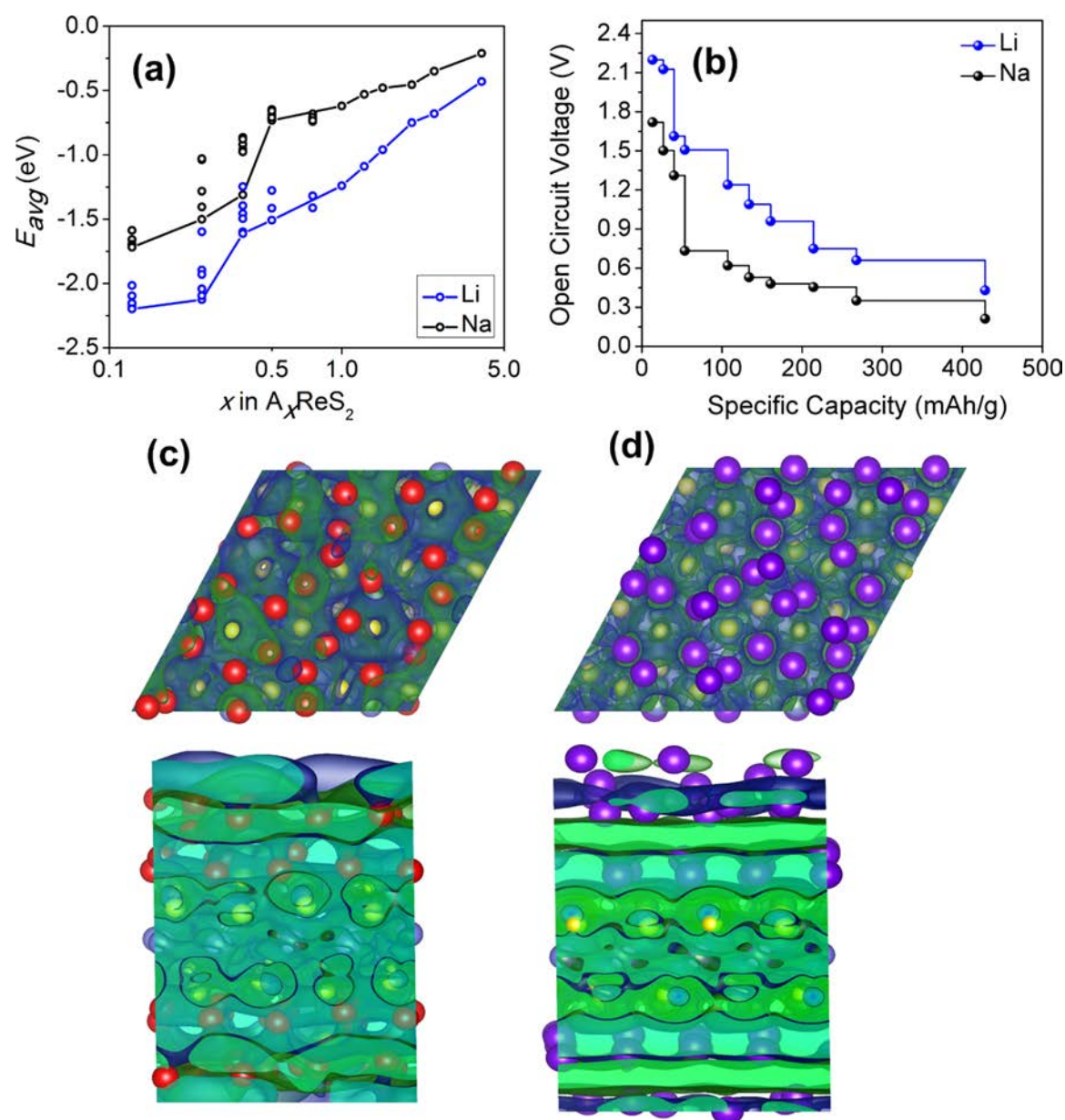




**Figure 3.** (Left) Projected density of states (PDOS) of the Li bound to (a) pristine, (b)  $V_S$ , (c)  $V_{2S}$ , and (d)  $V_{Re}$   $ReS_2$  systems. (Right) PDOS of the Na bound to (a) pristine, (b)  $V_S$ , (c)  $V_{2S}$ , and (d)  $V_{Re}$  systems. The Fermi energies for all plots were set to 0 eV.

428 mAh/g for both Li and Na. The average adsorption energies ( $E_{avg}$ ) are  $-0.43$  and  $-0.55$  eV for Li and Na,

respectively. When extra metal atoms are added over the substrate, they are either pushed away from the  $ReS_2$  surface or



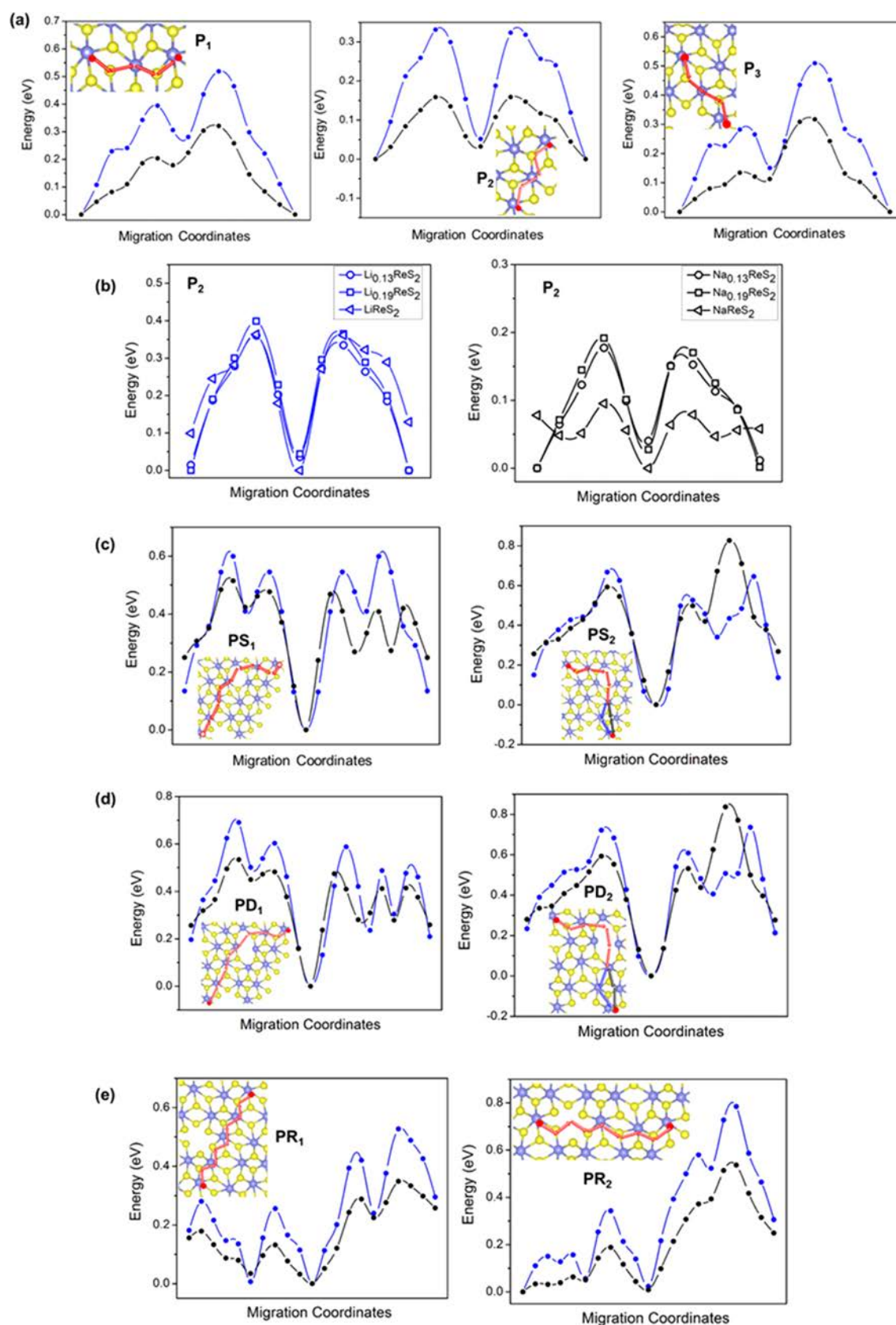
**Figure 4.** (a) Average adsorption energy as a function of Li/Na adsorption concentration. (b) Open-circuit voltage for Li/Na adatoms as a function of specific capacity. Top view and side view of charge density difference plots for (c)  $\text{Li}_4\text{ReS}_2$  and (d)  $\text{Na}_4\text{ReS}_2$ . Color code for atoms: yellow, S; blue, Re; red, Li; violet, Na. The isosurface level is set to be  $0.0002 \text{ e}/\text{\AA}^3$ . Green and light blue regions indicate charge accumulation and depletion, respectively.

the substrate experiences irreparable distortion. The open-circuit voltages as a function of specific capacity for Li and Na are shown in Figure 4a,b. It can be noted that the voltage profiles of  $\text{ReS}_2$  for increasing concentrations of Li and Na are similar to those of graphene,<sup>34,38</sup> 2D  $\text{MoS}_2$ ,  $\text{VS}_2$  nanocomposite,<sup>47</sup>  $\text{Ti}_3\text{C}_2$ ,<sup>48</sup>  $\text{GeS}$ ,<sup>50</sup> and other 2D materials,<sup>13,54</sup> and the low values indicate its suitability as an anode material in both cases. The charge density difference plots for  $\text{Li}_4\text{ReS}_2$  and  $\text{Na}_4\text{ReS}_2$  are shown in Figure 4c,d. The specific capacity of 428 mAh/g is in excellent agreement with 427 mAh/g measured experimentally by Qi et al.<sup>22</sup> Additionally, they demonstrated that the capacity of bare  $\text{ReS}_2$  can be further improved to 1048 mAh/g with a high capacity retention of 93.6% after 100 cycles by creating a  $\text{ReS}_2$ - and carbon nanotube-based composite. Additionally, although the specific capacity of  $\text{ReS}_2$  for Li intercalation is better than that of monolayer  $\text{GeS}$  (256 mAh/

g), the specific capacity of 428 mAh/g for Na is poorer than  $\text{GeS}$  (512 mAh/g).<sup>50</sup>

**3.3. Diffusion of Li and Na on Pristine and Defective  $\text{ReS}_2$  Surface.** The performance of the anode material in alkali-metal-ion batteries is determined by the competition between adsorption and diffusion of ions over substrate. From a purely thermodynamic standpoint, the alkali atoms would want to migrate from the most favorable adsorption site of one unit cell to their counterparts in the neighboring unit cells. It is well known that the charging/discharging rate depends on the mobility of alkali ions in the anode of the battery. In most 2D materials, such as  $\text{MoS}_2$ , graphene, phosphorene, and metallic carbides, the overall structure is highly symmetric and a small diffusion pathway is representative of the overall diffusion pathways in the material. In  $\text{ReS}_2$ , however, the structural anisotropy and lack of symmetry create more unique pathways





**Figure 5.** Diffusion of Li (blue) and Na (black) over pristine and defective  $\text{ReS}_2$ . Energy profile associated with the diffusion of (a) one isolated Li atom and one isolated Na atom over pristine  $\text{ReS}_2$ , (b) a range of concentrations of Li and Na over pristine  $\text{ReS}_2$ , one isolated Li atom and one isolated Na atom over, (c)  $V_S$ , (d)  $V_{2S}$ , and (e)  $V_{Re}$ . The red circles represent initial and final positions of the diffusing atoms used for the NEB calculations. The arrows in the insets show the mean energy pathways (MEPs) of diffusing atoms. The red arrows represent the common migration path for both Li and Na atoms, whereas the blue and black arrows represent individual paths for Li and Na when they are not identical.



for diffusion to occur. Essentially, Li and Na ions can diffuse over Re chains and S chains. Therefore, from a kinetics standpoint, to accurately find the most favored diffusion pathways and the associated activation energy barriers ( $E_a$ ), we simulated longer diffusion pathways.

Here, the energy barriers associated with the diffusion of Li atoms over pristine and defective  $\text{ReS}_2$  monolayers are reported. For pristine  $\text{ReS}_2$ , diffusion of Li and Na atoms was considered in three different directions, i.e., NEB simulations were performed to find the energy barriers associated with the migration of a Li and a Na atom from site-A to their counterparts in neighboring unit cells in a  $2 \times 2$  supercell. Schematics of the minimum-energy pathways (MEPs) and corresponding energy barriers as a function of diffusion paths are plotted in Figure 4a. Similarly, the MEPs and the energy barriers for the diffusion of Li from site-B are presented in Figure S6. For Li, the diffusion barrier for path  $P_2$  is 0.33 eV, whereas for both  $P_2$  and  $P_3$ , the value is 0.51 eV. These numbers are in excellent agreement with an energy barrier of 0.39 eV for Li diffusion in pristine  $\text{ReS}_2$  reported earlier.<sup>23</sup> On the other hand, for Na diffusion, the magnitudes of  $E_a$  for paths  $P_1$ ,  $P_2$ , and  $P_3$  are 0.31, 0.16, and 0.32 eV, respectively. The difference in the binding energy between site-A and site-B is merely 0.1 eV for Li and 0.04 eV for Na, causing a similar adsorption energy along the furrows and smaller diffusion energy barrier for path  $P_2$ . It is obvious that the diffusion of a Li atom on perfect  $\text{ReS}_2$  is not isotropic, which is due to the inherent lack of structural and electronic symmetry. However, because the energy barrier for  $P_2$  is the smallest (path length  $\sim 6$  Å), 0.33 and 0.16 eV are the energy barriers for the diffusion of Li and Na over pristine  $\text{ReS}_2$ , respectively. To give these numbers some perspective, the diffusion barriers of Li over graphene, phosphorene,  $\text{MoS}_2$ , flat borophene, GeS, and  $\text{Ti}_3\text{C}_2$  MXene are 0.37,<sup>55</sup> 0.13–0.76,<sup>56</sup> 0.24,<sup>35</sup> 0.69,<sup>57</sup> 0.24,<sup>50</sup> and 0.7 eV,<sup>48</sup> respectively. Similarly, the barrier heights for Na diffusion over graphene, flat borophene, GeS, and phosphorene are 0.19,<sup>37</sup> 0.34,<sup>57</sup> 0.09,<sup>50</sup> and 0.04 eV,<sup>58</sup> respectively. Low energy barriers for Li and Na diffusion over pristine  $\text{ReS}_2$  indicates its fast charge–discharge capabilities for AIBs.

To find the effect of adatom concentration on the diffusion, we performed CI-NEB simulations for three other concentrations of Li and Na. Because  $P_2$  was earlier found to be the lowest energy diffusion pathway, these additional simulations were therefore performed for the same pathway. Associated energy profiles are shown in Figure 4b. The compositions of the systems were  $\text{A}_{0.13}\text{ReS}_2$ ,  $\text{A}_{0.19}\text{ReS}_2$ , and  $\text{AReS}_2$ , where  $\text{A} = \text{Li}$  and  $\text{Na}$ . The results from our simulations are interesting. Initially, as the adatom concentration is increased, the energy barriers slightly increase for both Li and Na. For example, the energy barriers for  $\text{Li}_{0.13}\text{ReS}_2$  and  $\text{Li}_{0.19}\text{ReS}_2$  are 0.36 and 0.39 eV, respectively, compared to the energy barrier of 0.33 eV for the system  $\text{Li}_{0.0625}\text{ReS}_2$ . Similarly, for  $\text{Na}_{0.13}\text{ReS}_2$  and  $\text{Na}_{0.19}\text{ReS}_2$ , the energy barriers to diffusion are 0.17 and 0.19 eV, respectively, compared to the energy barrier of 0.16 eV for the  $\text{Na}_{0.0625}\text{ReS}_2$ . Interestingly, as the concentration of Li/Na is increased further, while the energy barrier for Li diffusion remains unchanged, the barrier for Na diffusion reduces dramatically. For example, the barrier for Li diffusion in the system  $\text{LiReS}_2$  is only 0.36 eV; however, the barrier to Na diffusion is a meager 0.09 eV in  $\text{NaReS}_2$ . These results indicate that for an LIB containing  $\text{ReS}_2$  as anode material, the rate of charging/discharging will not change with increasing concen-

trations of Li, but the rate will increase considerably with Na concentration in  $\text{ReS}_2$ -based NIBs.

Although strong adsorption energies achieved by the introduction of lattice defects are desirable for the alkali atom in anode materials, too high of a binding energy can inhibit the atomic motion and diffusion. With large adsorption energies, the defective sites sometimes essentially act as traps and consequently the associated diffusion barriers can increase sharply. For defective  $\text{ReS}_2$ , we have simulated the entire diffusion pathways, including confinement of the alkali atoms in the vicinity of the defective sites and their escape from the defective regions. Our NEB simulations of minimum-energy pathways for Li and Na diffusion suggest that  $V_S$ ,  $V_{2S}$ , and  $V_{Re}$  trap the alkali-metal atoms to different degrees and as a result increase the diffusion energy barriers compared to the defect-free case. As shown before,  $V_S$  is the most probable point defect to form in monolayer  $\text{ReS}_2$  under both Re- and S-rich conditions. Therefore, the effect of  $V_S$  on diffusion is discussed first. Similar to pristine  $\text{ReS}_2$ , for  $V_S$  also, two distinct migration paths across the defective site have been considered. The energy barriers for escaping the defective site are relatively larger than that of pristine  $\text{ReS}_2$ . As shown in Figure 4c, the diffusion barrier increases to 0.55 eV for Li and 0.47 eV for Na, as the alkali atoms migrate along path  $PS_1$  escaping  $V_S$ , whereas it increases to 0.67 eV for Li and 0.59 eV for Na along  $PS_2$ . Similarly, for  $V_{2S}$  (Figure 4d), we considered two migration paths, namely,  $PD_1$  and  $PD_2$ . As shown in Figure 4d, the energy barriers for diffusion along  $PD_1$  and  $PD_2$  were 0.72 and 0.6 eV for Li and 0.59 and 0.48 eV for Na, respectively. It is noteworthy that the diffusion energy barrier is comparatively small in the vicinity of the defect, whereas it is significantly large when escaping the defective site. This effect has been observed before in defective monolayer black phosphorus.<sup>38</sup> Finally, for  $V_{Re}$  (Figure 4e), two diffusion paths were considered, namely, path  $PR_1$  and  $PR_2$ . The diffusion barrier for path  $PR_1$  increases to 0.42 eV for Li and 0.28 eV for Na. On the other hand, for path  $PR_2$ , the energy barrier increases to 0.58 eV for Li and 0.54 eV for Na. Therefore, the largest increase in the energy barrier takes place when traversing a double vacancy, whereas the lowest increase in energy barrier happens near a Re single vacancy. From these values of migration energy barriers, it is evident that the diffusion of Li and Na atoms are difficult in defective  $\text{ReS}_2$  monolayers compared to pristine  $\text{ReS}_2$ . A summary of diffusion energy barriers for the migration of Li and Na over pristine,  $V_S$ ,  $V_{2S}$ , and  $V_{Re}$   $\text{ReS}_2$  is presented in Table 2.

**Table 2. Summary of Diffusion Energy Barriers for the Migration of Li and Na over Pristine,  $V_S$ ,  $V_{2S}$ , and  $V_{Re}$   $\text{ReS}_2$**

alkali metal	diffusion energy barrier (eV)			
	pristine	$V_S$	$V_{2S}$	$V_{Re}$
Li	0.33	0.55	0.60	0.42
Na	0.16	0.47	0.48	0.28

According to Arrhenius equation, the diffusion constant ( $D$ ) is given by

$$D \sim \exp\left(\frac{-E_a}{k_B T}\right) \quad (8)$$

where  $k_B$  is the Boltzmann constant and  $T$  is the operating temperature. The following predictions can be made using eq 8 (a) The diffusion of Na over pristine  $\text{ReS}_2$  is 700 times faster

than that of Li. (b) Although the presence of  $V_{\text{Re}}$  in pristine monolayer  $\text{ReS}_2$  reduces the diffusivity of Li atoms by a mere 32 times, the introduction of  $V_{\text{S}}$  and  $V_{2\text{S}}$  slows it down by  $5.3 \times 10^3$  and  $3.6 \times 10^3$  times. In case of Na, the diffusion over  $V_{\text{Re}}$ ,  $V_{\text{S}}$ , and  $V_{2\text{S}}$  can be  $1.06 \times 10^2$ ,  $1.7 \times 10^5$ , and  $2.6 \times 10^5$  times slower than pristine  $\text{ReS}_2$ , respectively. These results indicate that Li and Na atoms tend to migrate to the defective sites, and as a result, the energy barriers associated with the backward migration increase. Also, the presence of  $V_{\text{Re}}$  reduces the charging/discharging rates of  $\text{ReS}_2$ -based AIBs marginally, whereas the adsorption capacity of the  $\text{ReS}_2$  monolayer improves considerably. Although the introduction of  $V_{\text{S}}$  and  $V_{2\text{S}}$  defects increases the binding energy of Li atoms, they significantly reduce the diffusion rates of the atoms, especially in case of Na diffusion. Therefore, it is desirable to avoid their formation to retain the advantages of  $\text{ReS}_2$  for AIBs applications. These observations are contrary to those for  $V_{\text{S}}$  and  $V_{2\text{S}}$  containing  $\text{MoS}_2$ , wherein the effect of point defects on the energy barriers for Li diffusion is negligible. The concentrations of  $V_{\text{S}}$  and  $V_{2\text{S}}$  can be reduced by increasing their formation energies. Therefore, an increase in the chemical potential of S in the surrounding environment during the  $\text{ReS}_2$  fabrication process (CVD) could reduce the concentrations of  $V_{\text{S}}$  and  $V_{2\text{S}}$ . Similarly, a reduction in the concentration of Re in the surrounding should also facilitate the formation of Re single vacancy and discourage the formation of S-based defects. Additionally, research done on  $\text{MoS}_2$  monolayers shows that S atoms containing thiol-group-containing molecules get adsorbed at the S-vacancy sites post-treatment, resulting in the reinsertion of missing sulfur atom.<sup>59,60</sup> As a result of this treatment, disulfides are formed on the  $\text{MoS}_2$ , thereby alleviating the detrimental effects of S-based point defects. In conclusion, the presence of  $V_{\text{Re}}$  enhances the capacity of the  $\text{ReS}_2$ -based AIBs, without affecting their charging/discharging rates and hence is not detrimental to their battery performance.

#### 4. CONCLUSIONS

Single-layer rhenium disulfide is a unique material with distinctive, anisotropic electronic, mechanical, and optical properties and has the potential to be used as an anode material in alkali-metal-ion batteries. By performing density functional theory calculations, we have analyzed the adsorption and diffusional characteristics of two alkali metals, namely, Li and Na, on pristine and defective monolayer  $\text{ReS}_2$ . Our studies show that Li and Na atoms can be adsorbed over pristine  $\text{ReS}_2$  with binding energies of  $-2.28$  and  $-1.71$  eV, respectively, with several other potential adsorption sites for both. The diffusion of Li and Na over pristine  $\text{ReS}_2$  is anisotropic, with energy barriers of  $0.33$  and  $0.16$  eV, respectively. The energy barriers associated with escaping a S double vacancy and single vacancy are significantly large,  $0.6$  and  $0.51$  eV for Li and  $0.59$  and  $0.47$  eV for Na, which indicates slower migration and sluggish charging/discharging (by a factor of  $10^3$ – $10^5$  compared to pristine  $\text{ReS}_2$ ). However, the diffusion energy barrier over Re single vacancy was found to be merely  $0.42$  eV for Li and only  $0.28$  eV for Na. These results suggest that monolayer  $\text{ReS}_2$  with Re single vacancy adsorbs both Li and Na stronger than pristine  $\text{ReS}_2$ , with negligible negotiation with the charging/discharging rate of the battery, and therefore can be a suitable anode material. In fact, a proper combination of defects and topological disorders can generate more energetically favorable structures and provide ways for more efficient battery technologies.

#### ■ ASSOCIATED CONTENT

##### Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsami.7b13604.

Adsorption energy of Li/Na with vacuum, adsorption energy of Li/Na over pristine  $\text{ReS}_2$ , differential charge density plots, Bader charge analysis for Li/Na adsorption over pristine and defective  $\text{ReS}_2$ , and diffusion of Li over site-B (PDF)

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All of the authors contributed toward preparing the manuscript and have given approval to the current version.

##### Notes

The authors declare no competing financial interest.

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#### ■ REFERENCES

- (1) Idota, Y.; Kubota, T.; Matsufuji, A.; Maekawa, Y.; Miyasaka, T. Tin-Based Amorphous Oxide: A High-Capacity Lithium-Ion-Storage Material. *Science* **1997**, 276, 1395–1397.
- (2) Yoo, E.; Kim, J.; Hosono, E.; Zhou, H.-s.; Kudo, T.; Honma, I. Large Reversible Li Storage of Graphene Nanosheet Families for Use in Rechargeable Lithium Ion Batteries. *Nano Lett.* **2008**, 8, 2277–2282.
- (3) Ji, L.; Lin, Z.; Alcoutlabi, M.; Zhang, X. Recent developments in nanostructured anode materials for rechargeable lithium-ion batteries. *Energy Environ. Sci.* **2011**, 4, 2682–2699.
- (4) Chen, K.; Xue, D. Materials chemistry toward electrochemical energy storage. *J. Mater. Chem. A* **2016**, 4, 7522–7537.
- (5) Hwang, J.-Y.; Myung, S.-T.; Sun, Y.-K. Sodium-ion batteries: present and future. *Chem. Soc. Rev.* **2017**, 46, 3529–3614.
- (6) Deng, D. Li-ion batteries: basics, progress, and challenges. *Energy Sci. Eng.* **2015**, 3, 385–418.
- (7) Wang, G.; Shen, X.; Yao, J.; Park, J. Graphene nanosheets for enhanced lithium storage in lithium ion batteries. *Carbon* **2009**, 47, 2049–2053.
- (8) Yang, S.; Li, S.; Tang, S.; Dong, W.; Sun, W.; Shen, D.; Wang, M. Sodium adsorption and intercalation in bilayer graphene from density functional theory calculations. *Theor. Chem. Acc.* **2016**, 135, 164.
- (9) Zhong, H.-X.; Gao, S.; Shi, J.-J.; Yang, L. Quasiparticle band gaps, excitonic effects, and anisotropic optical properties of the monolayer distorted 1 T diamond-chain structures  $\text{ReS}_2$  and  $\text{ReSe}_2$ . *Phys. Rev. B* **2015**, 92, No. 115438.
- (10) Zhao, S.; Kang, W.; Xue, J. The potential application of phosphorene as an anode material in Li-ion batteries. *J. Mater. Chem. A* **2014**, 2, 19046–19052.



- (11) Kulish, V. V.; Malyi, O. I.; Persson, C.; Wu, P. Phosphorene as an anode material for Na-ion batteries: a first-principles study. *Phys. Chem. Chem. Phys.* **2015**, *17*, 13921–13928.
- (12) Jiang, H. R.; Lu, Z.; Wu, M. C.; Ciucci, F.; Zhao, T. S. Borophene: A promising anode material offering high specific capacity and high rate capability for lithium-ion batteries. *Nano Energy* **2016**, *23*, 97–104.
- (13) Rao, D.; Zhang, L.; Meng, Z.; Zhang, X.; Wang, Y.; Qiao, G.; Shen, X.; Xia, H.; Liu, J.; Lu, R. Ultrahigh energy storage and ultrafast ion diffusion in borophene-based anodes for rechargeable metal ion batteries. *J. Mater. Chem. A* **2017**, *5*, 2328–2338.
- (14) Tu, K.; Li, F.; Chen, Z. Enhanced lithium adsorption/diffusion and improved Li capacity on SnS<sub>2</sub> nanoribbons: A computational investigation. *J. Mater. Res.* **2016**, *31*, 878–885.
- (15) Li, Y.; Wu, D.; Zhou, Z.; Cabrera, C. R.; Chen, Z. Enhanced Li Adsorption and Diffusion on MoS<sub>2</sub> Zigzag Nanoribbons by Edge Effects: A Computational Study. *J. Phys. Chem. Lett.* **2012**, *3*, 2221–2227.
- (16) Stephenson, T.; Li, Z.; Olsen, B.; Mitlin, D. Lithium ion battery applications of molybdenum disulfide (MoS<sub>2</sub>) nanocomposites. *Energy Environ. Sci.* **2014**, *7*, 209–231.
- (17) Liu, Y.; Wang, W.; Wang, Y.; Peng, X. Homogeneously assembling like-charged WS<sub>2</sub> and GO nanosheets lamellar composite films by filtration for highly efficient lithium ion batteries. *Nano Energy* **2014**, *7*, 25–32.
- (18) Aslan, O. B.; Chenet, D. A.; van der Zande, A. M.; Hone, J. C.; Heinz, T. F. Linearly Polarized Excitons in Single- and Few-Layer ReS<sub>2</sub> Crystals. *ACS Photonics* **2016**, *3*, 96–101.
- (19) Cao, C.; Daly, M.; Chen, B.; Howe, J. Y.; Singh, C. V.; Filleter, T.; Sun, Y. Strengthening in graphene oxide nanosheets: bridging the gap between interplanar and intraplanar fracture. *Nano Lett.* **2015**, *15*, 6528–6534.
- (20) Tongay, S.; Sahin, H.; Ko, C.; Luce, A.; Fan, W.; Liu, K.; Zhou, J.; Huang, Y.-S.; Ho, C.-H.; Yan, J.; et al. Monolayer behaviour in bulk ReS<sub>2</sub> due to electronic and vibrational decoupling. *Nat. Commun.* **2014**, *5*, No. 3252.
- (21) Shi, F.; Song, Z.; Ross, P. N.; Somorjai, G. A.; Ritchie, R. O.; Komvopoulos, K. Failure mechanisms of single-crystal silicon electrodes in lithium-ion batteries. *Nat. Commun.* **2016**, *7*, No. 11886.
- (22) Qi, F.; He, J.; Chen, Y.; Zheng, B.; Li, Q.; Wang, X.; Yu, B.; Lin, J.; Zhou, J.; Li, P.; Zhang, W.; Li, Y. Few-layered ReS<sub>2</sub> nanosheets grown on carbon nanotubes: A highly efficient anode for high-performance lithium-ion batteries. *Chem. Eng. J.* **2017**, *315*, 10–17.
- (23) Zhang, Q.; Tan, S.; Mendes, R. G.; Sun, Z.; Chen, Y.; Kong, X.; Xue, Y.; Rummeli, M. H.; Wu, X.; Chen, S.; Fu, L. Extremely Weak van der Waals Coupling in Vertical ReS<sub>2</sub> Nanowalls for High-Current-Density Lithium-Ion Batteries. *Adv. Mater.* **2016**, *28*, 2616–2623.
- (24) Gao, J.; Li, L.; Tan, J.; Sun, H.; Li, B.; Idrobo, J. C.; Singh, C. V.; Lu, T.-M.; Koratkar, N. Vertically Oriented Arrays of ReS<sub>2</sub> Nanosheets for Electrochemical Energy Storage and Electrocatalysis. *Nano Lett.* **2016**, *16*, 3780–3787.
- (25) Chenet, D. A.; Aslan, O. B.; Huang, P. Y.; Fan, C.; van der Zande, A. M.; Heinz, T. F.; Hone, J. C. In-Plane Anisotropy in Mono- and Few-Layer ReS<sub>2</sub> Probed by Raman Spectroscopy and Scanning Transmission Electron Microscopy. *Nano Lett.* **2015**, *15*, 5667–5672.
- (26) Pradhan, N. R.; McCreary, A.; Rhodes, D.; Lu, Z.; Feng, S.; Manousakis, E.; Smirnov, D.; Namburu, R.; Dubey, M.; Hight Walker, A. R.; Terrones, H.; Terrones, M.; Dobrosavljevic, V.; Balicas, L. Metal to Insulator Quantum-Phase Transition in Few-Layered ReS<sub>2</sub>. *Nano Lett.* **2015**, *15*, 8377–8384.
- (27) Fujita, T.; Ito, Y.; Tan, Y.; Yamaguchi, H.; Hojo, D.; Hirata, A.; Voiry, D.; Chhowalla, M.; Chen, M. Chemically exfoliated ReS<sub>2</sub> nanosheets. *Nanoscale* **2014**, *6*, 12458–12462.
- (28) Al-Dulaimi, N.; Lewis, E. A.; Lewis, D. J.; Howell, S. K.; Haigh, S. J.; O'Brien, P. Sequential bottom-up and top-down processing for the synthesis of transition metal dichalcogenide nanosheets: the case of rhenium disulfide (ReS<sub>2</sub>). *Chem. Commun.* **2016**, *52*, 7878–7881.
- (29) Wu, K.; Chen, B.; Yang, S.; Wang, G.; Kong, W.; Cai, H.; Aoki, T.; Soignard, E.; Marie, X.; Yano, A.; Suslu, A.; Urbaszek, B.; Tongay, S. Domain Architectures and Grain Boundaries in Chemical Vapor Deposited Highly Anisotropic ReS<sub>2</sub> Monolayer Films. *Nano Lett.* **2016**, *16*, 5888–5894.
- (30) Zhang, T.; Jiang, B.; Xu, Z.; Mendes, R. G.; Xiao, Y.; Chen, L.; Fang, L.; Gemming, T.; Chen, S.; Rummeli, M. H.; Fu, L. Twinned growth behaviour of two-dimensional materials. *Nat. Commun.* **2016**, *7*, No. 13911.
- (31) Chaturvedi, A.; Slabon, A.; Hu, P.; Feng, S.; Zhang, K.-k.; Prabhakar, R. R.; Kloc, C. Rapid synthesis of transition metal dichalcogenide few-layer thin crystals by the microwave-induced-plasma assisted method. *J. Cryst. Growth* **2016**, *450*, 140–147.
- (32) Zhang, X.-O.; Li, Q.-F. Strain-induced magnetism in ReS<sub>2</sub> monolayer with defects. *Chin. Phys. B* **2016**, *25*, No. 117103.
- (33) Manchanda, P.; Skomski, R. Defect-induced magnetism in two-dimensional NbSe<sub>2</sub>. *Superlattices Microstruct.* **2017**, *101*, 349–353.
- (34) Datta, D.; Li, J.; Koratkar, N.; Shenoy, V. B. Enhanced lithiation in defective graphene. *Carbon* **2014**, *80*, 305–310.
- (35) Sun, X.; Wang, Z.; Fu, Y. Q. Defect-mediated lithium adsorption and diffusion on monolayer molybdenum disulfide. *Sci. Rep.* **2015**, *5*, No. 18712.
- (36) Zhou, L.-J.; Hou, Z. F.; Wu, L.-M.; Zhang, Y.-F. First-principles studies of lithium adsorption and diffusion on graphene with grain boundaries. *J. Phys. Chem. C* **2014**, *118*, 28055–28062.
- (37) Sun, X.; Wang, Z.; Fu, Y. Q. Adsorption and diffusion of sodium on graphene with grain boundaries. *Carbon* **2017**, *116*, 415–421.
- (38) Zhang, R.; Wu, X.; Yang, J. Blockage of ultrafast and directional diffusion of Li atoms on phosphorene with intrinsic defects. *Nanoscale* **2016**, *8*, 4001–4006.
- (39) Horzum, S.; Çakır, D.; Suh, J.; Tongay, S.; Huang, Y.-S.; Ho, C.-H.; Wu, J.; Sahin, H.; Peeters, F. M. Formation and stability of point defects in monolayer rhenium disulfide. *Phys. Rev. B* **2014**, *89*, No. 155433.
- (40) Perdew, J. P.; Burke, K.; Ernzerhof, M. Generalized Gradient Approximation Made Simple. *Phys. Rev. Lett.* **1996**, *77*, 3865–3868.
- (41) Giannozzi, P.; Baroni, S.; Bonini, N.; Calandra, M.; Car, R.; Cavazzoni, C.; Ceresoli, D.; Chiarotti, G. L.; Cococcioni, M.; Dabo, I.; Dal Corso, A.; Fabris, S.; Fratesi, G.; de Gironcoli, S.; Gebauer, R.; Gerstmann, U.; Gougousis, C.; Kokalj, A.; Lazzeri, M.; Martin-Samos, L.; Marzari, N.; Mauri, F.; Mazzarello, R.; Paolini, S.; Pasquarello, A.; Paulatto, L.; Sbraccia, C.; Scandolo, S.; Sclauzero, G.; Seitsonen, A. P.; Smogunov, A.; Umari, P.; Wentzcovitch, R. M. QUANTUM ESPRESSO: a modular and open-source software project for quantum simulations of materials. *J. Phys.: Condens. Matter* **2009**, *21*, No. 395502.
- (42) Monkhorst, H. J.; Pack, J. D. Special points for Brillouin-zone integrations. *Phys. Rev. B* **1976**, *13*, 5188–5192.
- (43) Kokalj, A. Computer graphics and graphical user interfaces as tools in simulations of matter at the atomic scale. *Comput. Mater. Sci.* **2003**, *28*, 155–168.
- (44) Momma, K.; Izumi, F. VESTA 3 for three-dimensional visualization of crystal, volumetric and morphology data. *J. Appl. Crystallogr.* **2011**, *44*, 1272–1276.
- (45) Barone, V.; Casarin, M.; Forrer, D.; Pavone, M.; Sami, M.; Vittadini, A. Role and effective treatment of dispersive forces in materials: Polyethylene and graphite crystals as test cases. *J. Comput. Chem.* **2009**, *30*, 934–939.
- (46) Peng, Q.; Wang, Z.; Sa, B.; Wu, B.; Sun, Z. Blue phosphorene/MS<sub>2</sub> (M = Nb, Ta) heterostructures as promising flexible anodes for lithium-ion batteries. *ACS Appl. Mater. Interfaces* **2016**, *8*, 13449–13457.
- (47) Samad, A.; Shin, Y.-H. MoS<sub>2</sub>@VS<sub>2</sub> nanocomposite as a superior hybrid anode material. *ACS Appl. Mater. Interfaces* **2017**, *9*, 29942–29949.
- (48) Er, D.; Li, J.; Naguib, M.; Gogotsi, Y.; Shenoy, V. B. Ti<sub>3</sub>C<sub>2</sub> MXene as a high capacity electrode material for metal (Li, Na, K, Ca) ion batteries. *ACS Appl. Mater. Interfaces* **2014**, *6*, 11173–11179.
- (49) Henkelman, G.; Uberuaga, B. P.; Jónsson, H. A climbing image nudged elastic band method for finding saddle points and minimum energy paths. *J. Chem. Phys.* **2000**, *113*, 9901–9904.

- (50) Li, F.; Qu, Y.; Zhao, M. Germanium sulfide nanosheet: a universal anode material for alkali metal ion batteries. *J. Mater. Chem. A* **2016**, *4*, 8905–8912.
- (51) Xiao, B.; Li, Y.-c.; Yu, X.-f.; Cheng, J.-b. Penta-graphene: A Promising Anode Material as the Li/Na-Ion Battery with Both Extremely High Theoretical Capacity and Fast Charge/Discharge Rate. *ACS Appl. Mater. Interfaces* **2016**, *8*, 35342–35352.
- (52) Meng, Q.; Hu, A.; Zhi, C.; Fan, J. Theoretical prediction of MXene-like structured  $\text{Ti}_3\text{C}_4$  as a high capacity electrode material for Na ion batteries. *Phys. Chem. Chem. Phys.* **2017**, *19*, 29106–29113.
- (53) Tang, W.; Sanville, E.; Henkelman, G. A grid-based Bader analysis algorithm without lattice bias. *J. Phys.: Condens. Matter* **2009**, *21*, No. 084204.
- (54) Meng, Q.; Hu, A.; Zhi, C.; Fan, J. Theoretical prediction of MXenes-like structure  $\text{Ti}_3\text{C}_4$  as a high capacity electrode material for Na ion batteries. *Phys. Chem. Chem. Phys.* **2017**, 29106.
- (55) Pollak, E.; Geng, B.; Jeon, K.-J.; Lucas, I. T.; Richardson, T. J.; Wang, F.; Kostecky, R. The Interaction of  $\text{Li}^+$  with Single-Layer and Few-Layer Graphene. *Nano Lett.* **2010**, *10*, 3386–3388.
- (56) Guo, G.-C.; Wei, X.-L.; Wang, D.; Luo, Y.; Liu, L.-M. Pristine and defect-containing phosphorene as promising anode materials for rechargeable Li batteries. *J. Mater. Chem. A* **2015**, *3*, 11246–11252.
- (57) Mortazavi, B.; Rahaman, O.; Ahzi, S.; Rabczuk, T. Flat borophene films as anode materials for Mg, Na or Li-ion batteries with ultra high capacities: A first-principles study. *Appl. Mater. Today* **2017**, *8*, 60–67.
- (58) Kulish, V. V.; Malyi, O. I.; Persson, C.; Wu, P. Adsorption of metal adatoms on single-layer phosphorene. *Phys. Chem. Chem. Phys.* **2015**, *17*, 992–1000.
- (59) Förster, A.; Gemming, S.; Seifert, G.; Tománek, D. Chemical and Electronic Repair Mechanism of Defects in  $\text{MoS}_2$  Monolayers. *ACS Nano* **2017**, *11*, 9989–9996.
- (60) Yu, Z.; Pan, Y.; Shen, Y.; Wang, Z.; Ong, Z.-Y.; Xu, T.; Xin, R.; Pan, L.; Wang, B.; Sun, L. Towards Intrinsic Charge Transport in Monolayer Molybdenum Disulfide by Defect and Interface Engineering. 2014, arXiv preprint arXiv:1408.6614. arXiv.org e-Printarchive. <http://arxiv.org/abs/1408.6614>.