Adsorption and Diffusion of Lithium and Sodium on Defective Rhenium Disulfide: A First Principles Study

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Supporting Information

ABSTRACT: Single-layer rhenium disulfide (ReS2) is a unique material with distinctive, anisotropic electronic, mechanical, and optical properties and has the potential to be used as an anode in alkali-metal-ion batteries. In this work, first principles calculations were performed to systematically evaluate the potential of monolayer pristine and defective ReS2 as anodes in lithium (Li)- and sodium (Na)-ion batteries. Our calculations suggest that there are several potential adsorption sites for Li and Na on pristine ReS2, owing to its low-symmetry structure. Additionally, the adsorption of Li and Na over pristine ReS2 is very strong with adsorption energies of −2.28 and −1.71 eV, respectively. Interestingly, the presence of point defects causes significantly stronger binding of the alkali-metal atoms with adsorption energies in the range −2.98 to −3.17 eV for Li and −2.66 to −2.92 eV for Na. Re single vacancy was found to be the strongest binding defect for Li adsorption, whereas S single vacancy was found to be the strongest for Na. The diffusion of these two alkali atoms over pristine ReS2 is anisotropic, with an energy barrier of 0.33 eV for Li and 0.16 eV for Na. The energy barriers associated with escaping a double vacancy and single vacancy for Li atoms are significantly large at 0.60 eV for the double-vacancy case and 0.51 eV for the single-vacancy case. Similarly, for Na, they are 0.59 and 0.47 eV, respectively, which indicates slower migration and sluggish charging/discharging. However, the diffusion energy barrier over a Re single vacancy is found to be merely 0.42 eV for a Li atom and 0.28 eV for Na. Overall, S single and double vacancies can reduce the diffusion rate by 10^{3}−10^{5} times for Li and Na ions, respectively. These results suggest that monolayer ReS2 with a Re single vacancy adsorbs Li and Na stronger than pristine ReS2, with negligible negotiation with the charging/discharging rate of the battery, and therefore they can be used as an anode in Li- and Na-ion batteries.

KEYWORDS: Li/Na-ion battery, density functional theory, ReS2, specific capacity, adsorption and diffusion

1. INTRODUCTION

With the ever-increasing demand for light, and eco-friendly batteries with high power and energy densities,1,2 low self-discharge rate, and comparatively long-term cycling stability3 for running mobile devices and electrical vehicles (EVs), scientists are in constant search of suitable electrode materials. Alkali-metal (Li, Na)-ion batteries (AIBs) are potential candidates for the next-generation energy technology as they are portable, energy-efficient, and environmentally friendly.4,5 The challenge associated with applying alkali-metal-ion batteries to EVs and portable appliances is obtaining a large storage capacity without compromising their long cycle lives and high charging/discharging rates.6 The latter is determined by the ionic mobilities of alkali-metal ions in the electrode materials of the battery, which depend on the electronic interactions between the electrode and the alkali-metal ion. Thus, performance of these batteries is primarily dependent on the quality of the electrodes used. The performance of commercial lithium-ion batteries (LIBs), which use graphitic materials, oxides, and oxysalts as anode materials, is limited due to their poor power density arising from the low diffusivity of Li atoms within them. Practical solutions to some of these problems is to use anode materials with large surface areas and high Li atom diffusivities. In this regard, theoretical and experimental studies have reported that two-dimensional (2D) materials can be effectively used as anode materials in AIBs due to their large surface-to-volume ratios and exceptional electronic and mechanical properties. For example, alkali-
metal-ion batteries with anodes based of 2D materials, such as graphene,7,8 phosphorene9–11 and borophene,12,13 have been investigated because of their excellent electrochemical performance as battery electrodes. In particular, graphene anodes have been demonstrated to possess capacities in the range of 600 mAh/g compared to a theoretical capacity of 372 mAh/g for graphite-based LIBs.7

In the recent past, 2D transition-metal dichalcogenides (TMDs), which combine transition metals and chalcogenides, have attained increased attention from the electrode development community.14–17 TMDs are layered structures, wherein different layers are held together by weak van der Waals forces. Unlike other 2D TMDs, ReS2 has a direct band gap (1.47–1.61 eV)18 and demonstrates a naturally distorted octahedral (1T) structure with a triclinic lattice, which provides unique chemical and electronic properties due to the lowered structural symmetry.19 In bulk ReS2, different atomic layers act electronically and vibrationally dissociated. As a result, the interlayer spacing in 2D ReS2 is about 0.65–0.7 nm, compared to 0.33 nm for graphite, whereas the interlayer coupling energy is 18 meV compared to 460 meV in MoS2.20 Consequently, relatively large Li ions can migrate rapidly through ReS2 without significant volumetric expansion, a problem critical to Si-based LIB anodes.21 Recent experiments have demonstrated that LIBs made of ReS2/graphene composites and few layers of ReS2/carbon nanotube-based nanosheets possess capacities in the range of 300–900 mAh/g.22,23 Additionally, we have recently demonstrated that vertically oriented arrays of ReS2 nanosheets hold exceptional potential for use in Li–S batteries for energy storage.24

Ever since the discovery of monolayer ReS2,20 several top-down exfoliation-based techniques have been utilized for its synthesis, such as top-down mechanical exfoliation5,26 and intercalation exfoliation27 from its bulk counterparts. Additionally, chemical vapor deposition (CVD),28,29 chemical vapor transport,20,29 metal sulfurization30 and plasma-assisted method31 have all been successfully utilized to fabricate 2D ReS2. Generally, synthesis of 2D materials from bulk structures using deposition techniques or exfoliation comes at the cost of defects, and grain boundaries.29 Thus, these structural defects alter the mechanical and electronic properties of the 2D structure significantly. For example, CVD-grown MoS2 possesses inferior carrier mobility compared to their exfoliated counterparts. Also, point defects have been demonstrated to alter the magnetic properties of ReS232 and NbSe233 significantly. It has been reported that point defects in graphene34 and MoS235 increase the adsorption capability of Li ions and therefore increase the storage capacity of the battery. However, this increased adsorption strength can affect the diffusivity of the Li ions in the electrode due to increased chemical interaction between the substrate and the Li ions. For example, Sun et al.35 reported that Li ions diffusion rates remain almost unaffected in MoS2 with point defects and grain boundaries. In graphene, on the other hand, the rate of diffusion of Li atoms is more pronounced along a grain boundary compared to a direction perpendicular to the boundary.36 Additionally, the rate of diffusion of Na over grain boundaries in graphene is more preferable over pristine graphene.37 On the contrary, Zhang et al.36 reported that single vacancies and double vacancies block the migration of Li ions over black phosphorous. These contradictions with different materials have lead us to raise the question of how lattice defects influence the adsorption and charging/discharging rates of Li and Na atoms in ReS2-based batteries.

In this paper, the adsorption and diffusion of Li and Na atoms over ReS2 via first principles density function theory (DFT) calculations have been reported. To the best of our knowledge, the adsorption and diffusion of Li and Na over defective ReS2 have not been studied before. First, the favorable adsorption sites for the metal ions over pristine ReS2 were identified, followed by the favorable adsorption sites for defective ReS2 surfaces. Three distinct point defects, namely, sulfur single vacancy (SV), rhenum single vacancy, and sulfur double vacancy (DV), were created in the ReS2 monolayers. These vacancies have been created in accordance with a previous DFT study on the stability and formation of point defects in ReS2.25,55 Our calculations showed that binding energies for Li and Na atoms increase over defective ReS2 compared to pristine monolayers. Additionally, charge density difference analysis and partial density of states calculations were performed to gain further insights into the adsorption process and characterize the electronic properties of Li- and Na-stuffed ReS2 monolayers. Finally, climbing image nudged elastic band (CI-NEB) simulations were performed to determine the minimum-energy pathways (MEPs) and associated energy barriers for the Li and Na atoms adsorbed onto the surface of ReS2.

2. COMPUTATIONAL METHODS

Plane-wave-based DFT simulations were conducted using the Perdew–Burke–Ernzerhof (PBE) exchange-correlation functional within the generalized gradient approximation using the Quantum ESPRESSO package.46 In addition, the Heyd–Scuseria–Ernzerhof (HSE06) functional was used to compute the band gap of pristine ReS2. The atomic positions and lattice constants were optimized using the kinetic energy cutoff of 60 Ry for the wave functions and 480 Ry for the charge density, respectively. The convergence criterion of the self-consistent-field procedure was set to 1 × 10−6 Ry. To avoid any interlayer interactions between ReS2 surfaces from long-range van der Waals forces due to periodicity, a convergence test with respect to the box dimension in the z direction was performed (see Table S1), and a vacuum spacing of 15 Å was deemed sufficient. For binding energy computations, the position of every atom was relaxed using a conjugate gradient minimization over a 4 × 4 × 1 Monkhorst–Pack61 grid of k-points with the residual Hellmann–Feynman force on each atom less than 0.001 Ry/Å. For structural analysis, all of the structures were visualized with XCRYSDEN63 and VESTA.64 The pristine ReS2 supercell consisted of 2 × 2 × 1 unit cells (with 48 atoms), whereas the single-vacancy (SV) and double-vacancy (DV) supercells consisted of 3 × 3 unit cells (107 and 106 atoms, respectively). When calculating the adsorption energies of adsorbents over pristine and defective ReS2, the dispersion corrections due to van der Waals forces were accounted for by adopting the DFT + D approach.50 To find the most stable adsorption positions, the alkali-metal atoms were placed above the sulfur atoms at different sites, followed by relaxation. The most stable adsorption site was determined by a comparison of the adsorption energies. The adsorption energy (Ead) and charge density difference (ρad) are determined by

\[ E_{ad} = E_{\text{adsorbed state}} - (E_{\text{adsorbent}} + E_{\text{substrate}}) \]  

\[ \rho_{ad} = \rho_{\text{adsorbed state}} - (\rho_{\text{adsorbent}} - \rho_{\text{substrate}}) \]

where \( E_{\text{adsorbed state}} \) represents the energy of monolayer ReS2 after the adsorption of an alkali-metal atom, \( E_{\text{adsorbent}} \) represents the energy of a single alkali-metal atom, and \( E_{\text{substrate}} \) represents the energy of the monolayer ReS2. A negative adsorption energy indicates that the adsorption is spontaneous and energetically favorable, with smaller values suggesting a stronger binding. Similarly, \( E_{\text{adsorbent}} \) is the...
The charge density of ReS$_2$ monolayer after alkali-metal adsorption, $\rho_{\text{adsorbent}}$ is the charge density of an alkali-metal atom, and $\rho_{\text{substrate}}$ represents the charge density of monolayer ReS$_2$. The average adsorption energy ($E_{\text{avg}}$) is calculated using the following equation

$$E_{\text{avg}} = \frac{E_{\text{adsorbed state}} - n \times E_{\text{adsorbed state}}}{n} - E_{\text{substrate}}$$  \hspace{1cm} (3)

where $n$ represents the number of Li and Na atoms adsorbed, $E_{\text{adsorbed state}}$ represents the energy of the system after adsorption of all of the Li/Na atoms, $n \times E_{\text{adsorbed state}}$ represents the total energy of the Li or Na atoms, and $E_{\text{substrate}}$ represents the energy of pristine ReS$_2$. The open-circuit voltage (OCV) of the secondary battery is related to the total energy storage of the battery. As shown in previous works, this parameter may be estimated using the following relation under the assumption that volume and entropic terms are negligible$^{46-48}$

$$\text{OCV} \approx -\frac{E_{\text{avg}}}{e}$$ \hspace{1cm} (4)

where $e$ is the elementary charge. The storage capacity of ReS$_2$ can be calculated using Faraday's equation, given by

$$q = 1000 \times F \times \frac{n}{M_{\text{ReS}_2}}$$ \hspace{1cm} (5)

where $F$, $n$, $M_{\text{ReS}_2}$, and $z$ are Faraday's constant, the number of electrons involved in the electrochemical reaction, the mass of ReS$_2$, and the number of valence electrons involved in the electrochemical process, respectively. For studying the kinetics of diffusion of the adsorbent atoms over pristine and defective ReS$_2$ monolayers and calculating the associated energy barriers of diffusion, the climbing image nudged elastic band (CI-NEB) method$^{49}$ was utilized.

3. RESULTS AND DISCUSSION

3.1. Structure of Pristine and Defective ReS$_2$. Before discussing distinctive characteristics of alkali-metal adsorption over pristine and defective ReS$_2$, their relative stabilities and structural aspects are presented here. Unlike other TMDs, which have stable 1H (dichalcogens of Mo and W) and 1T (dichalcogens of Ti, V, and Ta) phases, ReS$_2$ has a distorted (1Td) phase, wherein four Re atoms group into Re$_4$ units to form ReS$_2$. Tongay et al. calculated the phonon dispersion using the PBE functional and compared the results with experimental measurements of Raman spectra in ReS$_2$. Additionally, unlike other transition-metal dichalcogenides (TMDs), the LA and ZA phonon modes of periodic 1H and 1T structures of ReS$_2$ have imaginary frequencies and therefore are dynamically unstable. The distorted structure of 2D ReS$_2$ provides unique chemical and electronic properties.

The distortion creates rhenium–sulfide bonds of varying lengths, with no single sulfur atom being in direct alignment with the ones surrounding it. In this study, the optimized parameters of the ReS$_2$ unit cell (Figure 1a) were found to be: $O_X = 6.54 \, \text{Å}$, $O_Y = 6.44 \, \text{Å}$, and $\angle XOY = 61.15^\circ$. The band diagram for pristine ReS$_2$ is shown in Figure 1b, which suggests a band gap of 1.43 eV. This band gap of ReS$_2$ is in excellent agreement with previous reports.$^{20}$ Because the PBE functional is known to underestimate band gap, HSE06 hybrid functional was used to obtain a more accurate electronic structure, which yielded a band gap of 2.41 eV for pristine ReS$_2$.

Due to its distorted structure, creating a defect at one site on the ReS$_2$ surface is not the same as creating a defect at another site. Thus, ReS$_2$ can have a vast variety of single and double vacancies of S and Re. Notably, whenever a vacancy defect is introduced on the ReS$_2$ surface, a substantial change in the overall structure occurs. The energetics and lattice structures of

Figure 1. (a) Top view and side view of the unit cell of ReS$_2$. (b) Band structure of pristine ReS$_2$, with a band gap of 1.43 eV. Configurations of point defects in monolayer ReS$_2$: Top view of optimized structures of (c) $V_S$, (d) $V_{2S}$, and (e) $V_{Re}$. Hollow circles represent S (yellow) and Re (blue) atoms removed from the monolayer ReS$_2$. (f) Formation energies associated with the lattice defects under both S-rich and Re-rich conditions.
point defects in anisotropic ReS₂ are distinct from those in isotropic binary honeycomb-like TMDs, such as MoS₂ and VSe₂. For example, using high-resolution transmission electron microscopy and Raman spectroscopy, Wu et al.29 identified and characterized the grain boundary structure in ReS₂ nanofilms and demonstrated that a variety of clusters and single, double, and triple vacancies are formed, which are complex in comparison to defect structures reported for other 2D systems. Commonly observed point defects in ReS₂ are monosulfur vacancy (V₁₂), disulfur vacancy (V₂₂), and single-metal vacancy (V₆₆). Horzum et al.30 systematically studied the energetics of different point defects in ReS₂ and found that the stability of the defects are site-dependent. They reported that the most stable single S vacancy in ReS₂ is obtained by removing a S atom from ReS chains (Figure 1c). The most stable V₂₂ is created by removing two S atoms from the same sublattice, i.e., by removing another S atom neighboring the V₁₂ (Figure 1d). Although two possible sites exist for creating V₆₆, the one with the lowest formation energy is shown in Figure 1e. The relative stability of different point defects in a system is determined in terms of the formation energy of the defect, which is given by

\[ E_f = E_{\text{def}} - E_{\text{pristine}} + \sum_i N \mu_i \]

(6)

where \( E_{\text{def}} \) and \( E_{\text{pristine}} \) are the total energies of the defective and pristine supercells, \( N \) is the number of \( i \)th atoms removed from the pristine surfaces to create defects, and \( \mu_i \) is the chemical potential of the \( i \)th species in its stable bulk form. Under thermal equilibrium, the chemical potential of ReS₂ monolayer satisfies \( \mu_{\text{ReS}_2} = \mu_{\text{Re}} + 2\mu_{\text{S}} \) where \( \mu_{\text{Re}} \) and \( \mu_{\text{S}} \) are the chemical potentials for Re and S, respectively. For a Re-rich environment, \( \mu_{\text{Re}} = E_{\text{tot}}(\text{Re}) \), where \( E_{\text{tot}}(\text{Re}) \) is the total energy of a Re atom in the bulk form. Thus, \( \mu_{\text{S}} = (\mu_{\text{ReS}_2} - \mu_{\text{Re}})/2 \). Under S-rich condition, \( \mu_{\text{S}} = E_{\text{tot}}(\text{S}) \), where \( E_{\text{tot}}(\text{S}) \) is the energy of a S atom in the bulk form. Therefore, \( \mu_{\text{ReS}_2} \) can be calculated as \( \mu_{\text{ReS}_2} = \mu_{\text{Re}} + 2\mu_{\text{S}} \) - 2\( \mu_{\text{S}} \). The formation energies for V₁₂, V₂₂, and V₆₆ are 1.18, 2.61, and 4.9 eV under S-rich conditions and 2.14, 4.53, and 3.02 eV under Re-rich condition, respectively (Figure 1f). These magnitudes of formation energies agree with those reported in ref 39. The formation energy of V₁₂ is the lowest under both Re-rich and S-rich conditions, which suggests that sulfur single vacancies are most likely to form during mechanical exfoliation. This behavior is similar to MoS₂, in which V₁₂ is the most energetically favored point defect but is unlike graphene, wherein carbon double vacancy is the most favored point defect. Also, since the formation energy of V₂₂ is larger than twice that of V₁₂, two separate V₁₂ would not combine to create a disulfur V₂₂ vacancy. Additionally, the Re single vacancy has the largest formation energy compared to V₁₂ even under a S-rich condition. At a finite temperature, \( T \), the areal density of defects is related to the formation energy of the defect and can be calculated using an Arrhenius-type equation given by

\[ N_{\text{defect}} = N_{\text{pristine}} \exp\left(\frac{-E_f^*}{k_bT}\right) \]

(7)

where \( N_{\text{pristine}} \) is the areal density of atoms in the pristine material, \( E_f^* \) is the formation energy of the defect at \( T \), \( k_b \) is the Boltzmann constant. Temperature-dependent magnitudes of \( E_f^* \) can be calculated by performing ab initio molecular dynamics simulations.

3.2. Adsorption of Li and Na on Pristine and Defective ReS₂. Pristine ReS₂ is anisotropic, which gives rise to several asymmetric adsorption sites favorable for lithiation and sodiation. The binding energies for the adsorption of Li and Na atoms for a set of 10 active sites over monolayer pristine ReS₂ surface have been evaluated. The equilibrium positions for Li and Na atoms were determined by first placing the adatoms 3.5 Å away from the ReS₂ surface and subsequently optimizing...
the structure by minimizing the overall energy. DFT calculations show that site-A with $E_{ad} = -2.28$ eV for Li and $-1.71$ eV for Na is the most favorable location for both lithiation and sodiation over pristine ReS$_2$. The metal atoms prefer to reside near the area in between three sulfur atoms. For the adsorption of Li over site-B and site-C, the magnitudes of $E_{ad}$ are $-2.2$ and $-2.1$ eV, respectively. The adsorption energy of Li over site-A is $0.89$ eV higher than that of SnS$_2$, $0.26$ eV higher than that of GeS$_2$, $0.1$ eV higher than that of MoS$_2$. Similarly, the adsorption energy of Na over site-A is $1.3$ eV higher than that of pentagraphene, $0.35$ eV higher than that of GeS$_2$, and $0.2$ eV higher than that of Ti$_2$C$_6$. The adsorption energies for Na over site-B and site-C are $-1.67$ and $-1.61$ eV, respectively. Equilibrium configurations and binding energies of Li and Na adsorption over site-A, site-B, and site-C are also presented in Figure 2a,b, with the corresponding charge density difference contours presented in Figures S1 and S2. The binding energies of Li and Na over all of the 10 sites are presented in Table S2. Negative adsorption energies for a range of adsorption sites indicate that Li and Na storage over pristine ReS$_2$ is a spontaneous process, which is an essential requirement for alkali-metal-ion batteries. Also, the binding energy associated with the adsorption of Li and Na is the largest near the Re chains. Thus, the adatoms atoms tend to accumulate near these Re chains.

Previously studies of Li adsorption on 2D materials suggest that metal adatoms tend to get adsorbed adjacent to the defective zone because of the unused electrons from the dangling bonds. To find the best adsorption sites for Li and Na onto defective ReS$_2$, a host of initial positions for the adatoms were considered around the defective sites, the strongest adsorption sites, and the corresponding adsorption energies are shown in Figure 2c–f. On defective ReS$_2$, Li and Na atoms prefer to get adsorbed in the hollow site between two S atoms. For example, in the case of V$_x$ (Figure 2c), both Li and Na prefer to bind directly over the vacancy, suggesting it has taken the place of the sulfur atom. The binding energies for Li and Na over V$_x$ are $2.98$ and $2.92$ eV, respectively. In the case of V$_{2S}$ (Figure 2d), the metal atoms prefer to adsorb onto a similar position, with binding energies of $-3.12$ and $2.68$ eV for Li and Na, respectively. The adsorption of a Li atom over monolayer ReS$_2$ with a V$_{Re}$ (Figure 2e) is the strongest with a binding energy of $-3.17$ eV, compared to a binding energy of $-2.28$ eV for pristine ReS$_2$. However, in the case of V$_{Re}$, the metal atoms tend to get adsorbed over site-A close to V$_{Re}$ rather than the hollow site created by the vacancy. Binding energies, the shortest distance between the adsorbent atoms and the Re and S atoms in pristine and defective ReS$_2$ are presented in Table 1. Charge density difference contours for Li and Na adsorption over defective ReS$_2$ are presented in Figures S3 and S4.

Additionally, Bader charge analysis was conducted to quantify the charge-transfer process and understand the nature of interaction between the substrate (pristine and defective) and the adatoms, the details of which are presented in Figure S5.

To better understand the adsorption mechanism and ensure that the ideal electrode characteristics of ReS$_2$ are retained, the projected density of states (PDOS) of all bound systems were calculated, as shown in Figure 3. As Li and Na atoms adsorb over pristine, and defective ReS$_2$ monolayers, they provide some electronic states to each system and act as electron-donor species. The Li and Na 2s states are found deep in the conduction band, in all ReS$_2$ systems, at energy levels corresponding to the magnitude of their respective binding energies. The adsorption of Li and Na in turn pushes the Fermi level to higher energies, n-doping all of the ReS$_2$ systems. After the adsorption of Li and Na, the Fermi levels of pristine, V$_{Re}$ and V$_{2S}$ ReS$_2$ monolayers are found at the bottom of the conduction band, increasing the free-electron concentration, giving rise to n-type semiconducting monolayers. The adsorption of Na on the pristine ReS$_2$ monolayer also closes the band gap between the valence and conduction bands, decreasing it to $\sim 0.6$ eV. After the adsorption of Li and Na on the V$_{Re}$ ReS$_2$ monolayer, the Fermi level is found at the top of valence band. The adsorption of Li and Na atoms decreases the conducting hole concentration, due to the n-doping, pushing the Fermi level to higher energies. However, at higher Li and Na concentrations, the Fermi level can be expected to increase to the bottom of the conduction band, creating a n-type semiconducting monolayer, increasing the free-electron concentration. The increase in free-electron concentration in all ReS$_2$ monolayer systems may increase their electrical conductivity and potentially enhance their electrode performance.

Throughout the charging/discharging process, the concentration of the metallic ions in alkali-metal-ion batteries changes, resulting in compositional changes. Depending on the concentration of the alkali atoms, the adsorption sites vary, which is why it is important to study the effect of composition on the adsorption over pristine monolayer ReS$_2$. Additionally, for commercial purposes, the OCV is widely used for characterizing the performance of alkali-metal-ion batteries, such as the state of charge and health. OCV can be evaluated by estimating the voltage for a range of metal atoms stoichiometry. Here, to find $E_{avg}$ OCV, and specific capacity of pristine ReS$_2$ as a function of Li and Na concentration, a 2 $\times$ 2 supercell (16 Re atoms, 32 S atoms) is considered. Simulations were performed for a range of initial arrangements of Li and Na atoms. Initially, the adatoms were placed over site-A, site-B, or site-C away from each other to avoid interactions of the adsorbent atoms. All of the structures are then fully optimized. The alkali atoms can be adsorbed until the average binding energy of each Li atom reaches 0 eV; however, for larger concentrations of the alkali atoms, the Re–S bonds may become weak or can fail, and they cannot rebuild and the charging/discharging process becomes irreversible. Therefore, low alkali atom concentrations have been considered here. Different compositions of Li$_x$ReS$_2$ and Na$_x$ReS$_2$ were studied with $x$ taking on values of 0.125 $0.25$, 0.375, 0.5, 1, 1.25, 1.5, 2, 2.5, and 4. Simulations show that the electrostatic repulsive force between the metal atoms increases progressively as the number of adatoms is increased. This leads to increasingly weaker adsorption. The highest Li/Na concentration is a 4:1 ratio between the adatoms and ReS$_2$ (i.e., Li$_x$ReS$_2$ and Na$_x$ReS$_2$), which leads to a specific capacity of
428 mAh/g for both Li and Na. The average adsorption energies ($E_{avg}$) are $-0.43$ and $-0.55$ eV for Li and Na, respectively. When extra metal atoms are added over the substrate, they are either pushed away from the ReS$_2$ surface or

Figure 3. (Left) Projected density of states (PDOS) of the Li bound to (a) pristine, (b) $V_{S}$, (c) $V_{2S}$, and (d) $V_{Re}$ ReS$_2$ systems. (Right) PDOS of the Na bound to (a) pristine, (b) $V_{S}$, (c) $V_{2S}$, and (d) $V_{Re}$ systems. The Fermi energies for all plots were set to 0 eV.
the substrate experiences irreparable distortion. The open-circuit voltages as a function of specific capacity for Li and Na are shown in Figure 4a,b. It can be noted that the voltage profiles of ReS$_2$ for increasing concentrations of Li and Na are similar to those of graphene, 34,38 2D MoS$_2$, VS$_2$ nanocomposite, 47 Ti$_3$C$_2$, 48 GeS, 50 and other 2D materials, 13,54 and the low values indicate its suitability as an anode material in both cases. The charge density difference plots for Li$_4$ReS$_2$ and Na$_4$ReS$_2$ are shown in Figure 4c,d. The specific capacity of 428 mAh/g is in excellent agreement with 427 mAh/g measured experimentally by Qi et al. 22 Additionally, they demonstrated that the capacity of bare ReS$_2$ can be further improved to 1048 mAh/g with a high capacity retention of 93.6% after 100 cycles by creating a ReS$_2$- and carbon nanotube-based composite. Additionally, although the specific capacity of ReS$_2$ for Li intercalation is better than that of monolayer GeS (256 mAh/g), the specific capacity of 428 mAh/g for Na is poorer than GeS (512 mAh/g). 50

3.3. Diffusion of Li and Na on Pristine and Defective ReS$_2$ Surface. The performance of the anode material in alkali-metal-ion batteries is determined by the competition between adsorption and diffusion of ions over substrate. From a purely thermodynamic standpoint, the alkali atoms would want to migrate from the most favorable adsorption site of one unit cell to their counterparts in the neighboring unit cells. It is well known that the charging/discharging rate depends on the mobility of alkali ions in the anode of the battery. In most 2D materials, such as MoS$_2$, graphene, phosphorene, and metallic carbides, the overall structure is highly symmetric and a small diffusion pathway is representative of the overall diffusion pathways in the material. In ReS$_2$, however, the structural anisotropy and lack of symmetry create more unique pathways.
Figure 5. Diffusion of Li (blue) and Na (black) over pristine and defective ReS₂. Energy profile associated with the diffusion of (a) one isolated Li atom and one isolated Na atom over pristine ReS₂, (b) a range of concentrations of Li and Na over pristine ReS₂, one isolated Li atom and one isolated Na atom over, (c) V₁, (d) V₂₀, and (e) V₃₀. The red circles represent initial and final positions of the diffusing atoms used for the NEB calculations. The arrows in the insets show the mean energy pathways (MEPs) of diffusing atoms. The red arrows represent the common migration path for both Li and Na atoms, whereas the blue and black arrows represent individual paths for Li and Na when they are not identical.
for diffusion to occur. Essentially, Li and Na ions can diffuse over Re chains and S chains. Therefore, from a kinetics standpoint, to accurately find the most favored diffusion pathways and the associated activation energy barriers (E\text{a}), we simulated longer diffusion pathways.

Here, the energy barriers associated with the diffusion of Li atoms over pristine and defective ReS\textsubscript{2} monolayers are reported. For pristine ReS\textsubscript{2}, diffusion of Li and Na atoms was considered in three different directions, i.e., NEB simulations were performed to find the energy barriers associated with the migration of a Li and a Na atom from site-A to their counterparts in neighboring unit cells in a 2 × 2 supercell. Schematics of the minimum-energy pathways (MEPs) and corresponding energy barriers as a function of diffusion paths are plotted in Figure 4a. Similarly, the MEPs and the energy barriers for the diffusion of Li from site-B are presented in Figure 56. For Li, the diffusion barrier for path P\textsubscript{2} is 0.33 eV, whereas for both P\textsubscript{1} and P\textsubscript{3}, the value is 0.51 eV. These numbers are in excellent agreement with an energy barrier of 0.39 eV for Li diffusion in pristine ReS\textsubscript{2} reported earlier.\textsuperscript{23} On the other hand, for Na diffusion, the magnitudes of E\text{a} for paths P\textsubscript{1}, P\textsubscript{2}, and P\textsubscript{3} are 0.31, 0.16, and 0.32 eV, respectively. The difference in the binding energy between site-A and site-B is merely 0.1 eV for Li and 0.04 eV for Na, causing a similar adsorption energy along the furrows and smaller diffusion energy barrier for path P\textsubscript{2}. It is obvious that the diffusion of a Li atom on perfect ReS\textsubscript{2} is not isotropic, which is due to the inherent lack of structural and electronic symmetry. However, because the energy barrier for P\textsubscript{2} is the smallest (path length ∼6Å), 0.33 and 0.16 eV are the energy barriers for the diffusion of Li and Na over pristine ReS\textsubscript{2}, respectively. To give these numbers some perspective, the diffusion barriers of Li over graphene, phosphorene, MoS\textsubscript{2}, flat borophene, GeS, and Ti\textsubscript{3}C\textsubscript{2} MXene are 0.37,\textsuperscript{55} 0.13−0.76,\textsuperscript{36} 0.24,\textsuperscript{55} 0.69,\textsuperscript{57} 0.24,\textsuperscript{50} and 0.7 eV\textsuperscript{48} respectively. Similarly, the barrier heights for Na diffusion over graphene, flat borophene, GeS, and phosphorene are 0.19,\textsuperscript{37} 0.34,\textsuperscript{35} 0.09,\textsuperscript{50} and 0.04 eV\textsuperscript{38} respectively. Low energy barriers for Li and Na diffusion over pristine ReS\textsubscript{2} indicates its fast charge−discharge capabilities for AIBs.

To find the effect of adatom concentration on the diffusion, we performed CI-NEB simulations for three other concentrations of Li and Na. Because P\textsubscript{2} was earlier found to be the lowest energy diffusion pathway, these additional simulations were therefore performed for the same pathway. Associated energy profiles are shown in Figure 4b. The compositions of the systems were A\textsubscript{0.13}ReS\textsubscript{2}, A\textsubscript{0.16}ReS\textsubscript{2}, and AReS\textsubscript{2}, where A = Li and Na. The results from our simulations are interesting. Initially, as the adatom concentration is increased, the energy barriers slightly increase for both Li and Na. For example, the energy barriers for Li\textsubscript{0.13}ReS\textsubscript{2} and Li\textsubscript{0.19}ReS\textsubscript{2} are 0.36 and 0.39 eV, respectively, compared to the energy barrier of 0.33 eV for the system Li\textsubscript{0.0625}ReS\textsubscript{2}. Similarly, for Na\textsubscript{0.13}ReS\textsubscript{2} and Na\textsubscript{0.16}ReS\textsubscript{2}, the energy barriers to diffusion are 0.17 and 0.19 eV, respectively, compared to the energy barrier of 0.16 eV for the Na\textsubscript{0.0625}ReS\textsubscript{2}. Interestingly, as the concentration of Li/Na is increased further, while the energy barrier for Li diffusion remains unchanged, the barrier for Na diffusion reduces dramatically. For example, the barrier for Li diffusion in the system Li\textsubscript{0.0625}ReS\textsubscript{2} is only 0.36 eV; however, the barrier to Na diffusion is a meager 0.09 eV in NaReS\textsubscript{2}. These results indicate that for an LIB containing ReS\textsubscript{2} as anode material, the rate of charging/discharging will not change with increasing concentrations of Li, but the rate will increase considerably with Na concentration in ReS\textsubscript{2}-based NIBs.

Although strong adsorption energies achieved by the introduction of lattice defects are desirable for the alkali atom in anode materials, too high of a binding energy can inhibit the atomic motion and diffusion. With large adsorption energies, the defective sites sometimes essentially act as traps and consequently the associated diffusion barriers can increase sharply. For defective ReS\textsubscript{2}, we have simulated the entire diffusion pathways, including confinement of the alkali atoms in the vicinity of the defective sites and their escape from the defective regions. Our NEB simulations of minimum-energy pathways for Li and Na diffusion suggest that V\textsubscript{5}, V\textsubscript{2S}, and V\textsubscript{Re} trap the alkali-metal atoms to different degrees and as a result increase the diffusion energy barriers compared to the defect-free case. As shown before, V\textsubscript{5} is the most probable point defect to form in monolayer ReS\textsubscript{2} under both Re- and S-rich conditions. Therefore, the effect of V\textsubscript{5} on diffusion is discussed first. Similar to pristine ReS\textsubscript{2}, for V\textsubscript{5} also, two distinct migration paths across the defective site have been considered. The energy barriers for escaping the defective site are relatively larger than that of pristine ReS\textsubscript{2}. As shown in Figure 4c, the diffusion barrier increases to 0.55 eV for Li and 0.47 eV for Na, as the alkali atoms migrate along path P\textsubscript{5S} escaping V\textsubscript{5}, whereas it increases to 0.67 eV for Li and 0.59 eV for Na along P\textsubscript{52}. Similarly, for V\textsubscript{2S} (Figure 4d), we considered two migration paths, namely, P\textsubscript{D1} and P\textsubscript{D2}. As shown in Figure 4d, the energy barriers for diffusion along P\textsubscript{D1} and P\textsubscript{D2} were 0.72 and 0.6 eV for Li and 0.59 and 0.48 eV for Na, respectively. It is noteworthy that the diffusion energy barrier is comparatively small in the vicinity of the defect, whereas it is significantly large when escaping the defective site. This effect has been observed before in defective monolayer black phosphorus.\textsuperscript{38} Finally, for V\textsubscript{Re} (Figure 5e), two diffusion paths were considered, namely, path PR\textsubscript{1} and PR\textsubscript{2}. The diffusion barrier for path PR\textsubscript{1} increases to 0.42 eV for Li and 0.28 eV for Na. On the other hand, for path PR\textsubscript{2}, the energy barrier increases to 0.58 eV for Li and 0.54 eV for Na. Therefore, the largest increase in the energy barrier takes place when traversing a double vacancy, whereas the lowest increase in energy barrier happens near a Re single vacancy. From these values of migration energy barriers, it is evident that the diffusion of Li and Na atoms are difficult in defective ReS\textsubscript{2} monolayers compared to pristine ReS\textsubscript{2}. A summary of diffusion energy barriers for the migration of Li and Na over pristine, V\textsubscript{5}, V\textsubscript{2S}, and V\textsubscript{Re} ReS\textsubscript{2} is presented in Table 2.

Table 2. Summary of Diffusion Energy Barriers for the Migration of Li and Na over Pristine, V\textsubscript{5}, V\textsubscript{2S}, and V\textsubscript{Re} ReS\textsubscript{2}

<table>
<thead>
<tr>
<th>alkali metal</th>
<th>pristine</th>
<th>V\textsubscript{5}</th>
<th>V\textsubscript{2S}</th>
<th>V\textsubscript{Re}</th>
</tr>
</thead>
<tbody>
<tr>
<td>Li</td>
<td>0.33</td>
<td>0.55</td>
<td>0.60</td>
<td>0.42</td>
</tr>
<tr>
<td>Na</td>
<td>0.16</td>
<td>0.47</td>
<td>0.48</td>
<td>0.28</td>
</tr>
</tbody>
</table>

According to Arrhenius equation, the diffusion constant (D) is given by

\[
D \sim \exp \left(\frac{-E_a}{k_B T}\right)
\]

(8)

where \(k_B\) is the Boltzmann constant and \(T\) is the operating temperature. The following predictions can be made using eq 8

(a) The diffusion of Na over pristine ReS\textsubscript{2} is 700 times faster

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than that of Li. (b) Although the presence of $V_{Re}$ in pristine monolayer ReS$_2$ reduces the diffusivity of Li atoms by a mere 32 times, the introduction of $V_{S}$ and $V_{SS}$ slows it down by $5.3 \times 10^3$ and $3.6 \times 10^3$ times. In case of Na$_x$, the diffusion over $V_{Re}$, $V_{S}$, and $V_{SS}$ can be $1.06 \times 10^3$, $1.7 \times 10^3$, and $2.6 \times 10^3$ times slower than pristine ReS$_2$, respectively. These results indicate that Li and Na atoms tend to migrate to the defective sites, and as a result, the energy barriers associated with the backward migration increase. Also, the presence of $V_{Re}$ reduces the charging/discharging rates of ReS$_2$-based AIBs marginally, whereas the adsorption capacity of the Re$_2$ monolayer improves considerably. Although the introduction of $V_{S}$ and $V_{SS}$ defects increases the binding energy of Li atoms, they significantly reduce the diffusion rates of the atoms, especially in case of Na diffusion. Therefore, it is desirable to avoid their formation to retain the advantages of ReS$_2$ for AIBs applications. These observations are contrary to those for $V_{S}$ and $V_{SS}$ containing MoS$_2$, wherein the effect of point defects on the energy barriers for Li diffusion is negligible. The concentrations of $V_{S}$ and $V_{SS}$ can be reduced by increasing their formation energies. Therefore, an increase in the chemical potential of S in the surrounding environment during the ReS$_2$ fabrication process (CVD) could reduce the concentrations of $V_{S}$ and $V_{SS}$. Similarly, a reduction in the concentration of Re in the surrounding should also facilitate the formation of Re single vacancy and discourage the formation of S-based defects. Additionally, research done on MoS$_2$ monolayers shows that S atoms containing thiol-group-containing molecules get adsorbed at the S-vacancy sites post-treatment, resulting in the reinsertion of missing sulfur atom. As a result of this treatment, disulfides are formed on the MoS$_2$, thereby alleviating the detrimental effects of S-based point defects. In conclusion, the presence of $V_{Re}$ enhances the capacity of the Re$_2$-based AIBs, without affecting their charging/discharging rates and hence is not detrimental to their battery performance.

4. CONCLUSIONS

Single-layer rhenium disulfide is a unique material with distinctive, anisotropic electronic, mechanical, and optical properties and has the potential to be used as an anode material in alkali-metal-ion batteries. By performing density functional theory calculations, we have analyzed the adsorption and diffusional characteristics of two alkali metals, namely, Li and Na, on pristine and defective monolayer ReS$_2$. Our studies show that Li and Na atoms can be adsorbed over pristine ReS$_2$ with binding energies of $-2.28$ and $-1.71$ eV, respectively, with several other potential adsorption sites for both. The diffusion of Li and Na over pristine ReS$_2$ is anisotropic, with energy barriers of 0.33 and 0.16 eV, respectively. The energy barriers associated with escaping a S double vacancy and single vacancy are significantly large, 0.6 and 0.51 eV for Li and 0.59 and 0.47 eV for Na, which indicates slower migration and sluggish charging/discharging (by a factor of $10^{-3}$ to $10^{-1}$ compared to pristine ReS$_2$). However, the diffusion energy barrier over Re single vacancy was found to be merely $0.28$ eV for Li and only $0.28$ eV for Na. These results suggest that monolayer ReS$_2$ with Re single vacancy adsorbs both Li and Na stronger than pristine ReS$_2$, with negligible negotiation with the charging/discharging rate of the battery, and therefore can be a suitable anode material. In fact, a proper combination of defects and topological disorders can generate more energetically favorable structures and provide ways for more efficient battery technologies.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsami.7b13604.

Adsorption energy of Li/Na with vacuum, adsorption energy of Li/Na over pristine ReS$_2$, differential charge density plots, Bader charge analysis for Li/Na adsorption over pristine and defective ReS$_2$, and diffusion of Li over site-B (PDF)

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All of the authors contributed toward preparing the manuscript and have given approval to the current version.

Notes

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